

1 **Experimental determination of porosity and permeability changes induced by massive**  
2 **injection of CO<sub>2</sub> into carbonate reservoirs.**

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11

12 **Abstract.** Coupled transport-reaction numerical simulations are essential to model large-scale  
13 processes over long durations. However, in the case of CO<sub>2</sub> underground storage, few  
14 experimental data exist allowing us to constrain and validate the various assumptions  
15 implemented in these models. In particular, little is known about the (irreversible)  
16 modifications of reservoir properties in the highly reactive systems resulting from massive  
17 CO<sub>2</sub> injection. A set of four reactive flow-trough experiments at temperature  $T = 100$  °C and  
18 total pressure  $P = 12$  MPa are performed using limestone reservoir samples. The objectives  
19 are to quantify mass transfers occurring (1) near the injection well, where the aquifer fluid is  
20 almost saturated with CO<sub>2</sub> (i.e.  $P_{CO_2} \approx P$ ), and (2) at increasing distances from the injection  
21 well, where the fluid is expected to display lower  $P_{CO_2}$  values and higher divalent cation  
22 concentrations resulting from rock dissolution along the fluid pathway.

1 The results for  $P_{CO_2}$  of 10 MPa and 6 MPa predict non-uniform dissolution features  
 2 associated with transport-controlled mass transfer near the injection well, while kinetically-  
 3 controlled uniform dissolution is observed at lower  $P_{CO_2}$  (2.5 MPa). Furthermore, the scaling  
 4 laws relating porosity to permeability are distinctly different between experiments. As a  
 5 result, macroscale porosity-permeability relationships should be parameterized not only to  
 6 account for rock-type-dependent properties, as is generally the case when modelling low  
 7 reactivity systems, but also to take account of the local dissolution regime. Therefore, we  
 8 define a reference macroscopic Damköhler number ( $Da^* = 1$ ) corresponding to the  
 9 kinetically-controlled dissolution conditions observed at  $P_{CO_2} = 2.5$  MPa. Then, the value of  
 10  $Da > 1$  characterizing the transport-controlled dissolution is given by the ratio between the  
 11 calcium production (normalized to the sample-size) obtained in experiments at  $P_{CO_2} > 2.5$   
 12 MPa and at  $P_{CO_2} = 2.5$  MPa. We propose a Damköhler-dependent relationship between  
 13 porosity and permeability:  $k \sim (\phi - \phi_c)^n$ , where  $\phi_c$  is the porosity at the percolation  
 14 threshold and  $n$  a power law of  $Da$ . As  $Da$  is defined only from macroscopic measurable  
 15 parameters (i.e. calcium concentration in the case of calcite dissolution), the proposed  $k - \phi -$   
 16  $Da$  law can be easily implemented in reservoir-scale numerical simulations. Finally, for the  
 17 experiment at  $P_{CO_2} = 0.7$ , i.e. reproducing conditions far from the injection well, we observe a  
 18 uniform decrease of the porosity associated with dolomitization of the reservoir. However, the  
 19 rate of permeability decrease is not constant but grows strongly as the porosity approaches  
 20  $\phi_c$ , indicating a probable clogging of the medium if dolomitization conditions persist.

21 Keywords: Geologic sequestration, carbon dioxide, hydrodynamic

22

## 1        **1 Introduction**

2        CO<sub>2</sub> sequestration in geological formations is increasingly being studied as a workable  
3 way of limiting the overload of CO<sub>2</sub> emissions in the atmosphere. CO<sub>2</sub> disposal into  
4 geological formations includes mainly deep-saline aquifers and depleted oil reservoirs, which  
5 represent storage capacities estimated around 10<sup>13</sup> kg and 4 x 10<sup>11</sup> kg, respectively (Holloway,  
6 1997). The process consists in injecting supercritical more-or-less-pure CO<sub>2</sub> into the  
7 formation porosity through boreholes, following the same procedure routinely performed by  
8 the petroleum industry for enhancing oil recovery. Here, we focus on carbonate-rich rocks  
9 which are widely present in sedimentary reservoirs.

10        Whatever the rock composition, the progressive dissolution of CO<sub>2</sub> in the formation water  
11 (generally at thermodynamic equilibrium with the rock-forming minerals) leads to a decrease  
12 in its pH. As a result, there is a significant increase in the dissolution capacity of the CO<sub>2</sub>-rich  
13 fluid and the main expected processes involve dissolution of carbonates and, eventually, the  
14 (alumino)silicates, depending on the kinetics of the individual reactions see reviews in  
15 Plummer et al. (1978) and Lasaga (1981). Near the injection well, where disequilibrium is  
16 maximal, dissolution processes are expected to affect (irreversibly) the mechanical and  
17 hydrodynamic properties of the host rock. Specifically, dissolution will lead to an increase in  
18 porosity and permeability as well as changes in the reactive surface. For a constant injection  
19 rate, the penetration distance of the dissolution front will be a complex function of all these  
20 time- and space-resolved modifications. Conversely, the increase of cation concentration  
21 produced by the carbonate dissolution will eventually produce supersaturated fluids with  
22 respect to carbonate minerals at the outermost front of the CO<sub>2</sub>-rich plume. We would expect  
23 precipitation processes and then decreasing porosity and permeability.

24        Several experimental and theoretical studies have analysed the geochemical reactions between  
25 reservoir rocks and injected carbon dioxide. Most of these studies investigated the mass

1 transfers of calcite, dolomite and magnesite, in contact with acid solutions at low CO<sub>2</sub> partial  
2 pressures (i.e.  $P_{\text{CO}_2} < 0.1$  MPa and room temperature (Lund et al., 1975; Plummer et al., 1978;  
3 Chou et al., 1989; Compton and Unwin, 1990; Dreybrodt et al., 1996; Arvidson et al., 2003;  
4 Noiriél et al., 2005). Others studies have focused on measuring calcite and dolomite  
5 dissolution rates at  $P_{\text{CO}_2} > 0.1$  MPa and/or moderate temperature ( $\leq 80^\circ\text{C}$ ) (Alkattan et al.,  
6 1998; Gautelier et al., 1999; Pokrovsky et al., 1999b). Recently, Pokrovsky et al. (2005)  
7 measured the dissolution rates of calcite, dolomite and magnesite as a function of  $P_{\text{CO}_2}$  ( $P_{\text{CO}_2}$   
8  $\leq 8$  MPa), at moderate NaCl concentration (0.01 to 1.0 M) and  $\text{pH} \leq 4$ . However, only few  
9 experimental studies have been published for  $P$ - $T$ - $P_{\text{CO}_2}$  conditions corresponding to the  
10 anticipated *in situ* conditions during injection, i.e.  $T = 80$ - $150$  °C and  $P = 9$ - $20$  MPa. For  
11 instance, Kaszuba et al. (2003, 2005) carried out dissolution/precipitation experiments at high  
12 temperature  $T = 200$  °C and high pressure ( $P = 20$  MPa) in a closed reactor using powdered  
13 rocks. These results are fundamental for understanding reaction paths and quantifying mass  
14 transfers in response to high  $P_{\text{CO}_2}$  fluids. Nevertheless, to quantify the long-lasting presence of  
15 huge volumes of CO<sub>2</sub> in reservoirs, we need to address the essential issue of feedback effects  
16 due to mass transfer, which can modify the pore structure and the hydrodynamic properties of  
17 the reservoir. Fluid-rock mass transfers depend on several parameters ( $P_{\text{CO}_2}$ , cation  
18 concentrations, flow rate or pressure head at the boundaries, reactive surface areas, porosity,  
19 permeability, tortuosity, etc). The behaviour of these coupled processes is unpredictable  
20 without the help of numerical modelling. However, a key difficulty remains the large  
21 variability of the characteristic scales and times of the hydrodynamic and chemical processes.  
22 Specifically, fluid flow and hydrodynamic transport are controlled by large-scale  
23 characteristics of the porous media (e.g. long-range correlation of the permeability field and  
24 boundary conditions), whereas chemical reactions are controlled by local parameters at the  
25 fluid mineral interfaces. Consequently, physics-based laws relating microscopic volume

1 changes to macroscopic changes in permeability are only available for very simple models of  
2 homogeneous porous media (i.e. stacked spheres). Otherwise, we need to make use of  
3 heuristic laws that simultaneously lump together and upscale all the processes relating mass  
4 transfer to hydrodynamic properties (Wong et al., 1984). At present, i.e. 70 years after the  
5 pioneering work of Kozeny (1927) and Carman (1937), most numerical models use power  
6 law permeability / porosity scaling for the reservoir to predict permeability changes triggered  
7 by fluid-rock mass transfers.

8 In carbonate-rich reservoirs, both the pore structure and the macro-scale distribution of the  
9 transport properties are complex as a result of many successive diagenetic events, whereas the  
10 chemical composition of the rock may be relatively simple. For highly reactive fluids such as  
11 high  $P_{\text{CO}_2}$  fluids, coupled flow and dissolution processes may induce the formation of highly  
12 conductive and spatially correlated flow channels, often termed wormholes (Fredd, 1998).

13 Wormholes grow because of the natural heterogeneity of the porous medium and the  
14 relatively fast dissolution of the carbonate phase under low pH conditions. Evidently, general  
15 laws relating permeability ( $k$ ) to porosity ( $\phi$ ) cannot account for changes in the spatial  
16 correlation of properties such as observed in the presence of wormholes.

17 This study aims to provide experimental data that can be used to constrain the modelling of  
18  $\text{CO}_2$  injection and sequestration, and specifically the permeability / porosity scaling law. We  
19 present a set of reactive percolation experiments carried out at pressures ( $P$ ) and temperatures  
20 ( $T$ ) typical of *in situ* conditions. Experiments are designed to quantify reactions occurring near  
21 the  $\text{CO}_2$  injection zone, where the aquifer fluid is saturated with  $\text{CO}_2$ . In addition, experiments  
22 were carried out at increasing distances from the injection point, where the fluid is expected to  
23 contain progressively less  $\text{CO}_2$  and more divalent cations resulting from rock dissolution  
24 along the fluid pathway. The underlying idea is to obtain experimental control-points in space  
25 and time corresponding to the transport of  $\text{CO}_2$  in the reservoir during the injection phase,

1 whereas a complete and continuous reproduction of these processes is clearly not feasible at  
2 the laboratory scale. The experimental protocol allows us to study the feedback between  
3 changes in porosity, permeability and rock structure induced by the mass transfer of rock-  
4 forming minerals due to reactive fluid percolation in the rock. The methodology combines  
5 chemical analysis of the fluid, continuous measurements of sample permeability and pore-  
6 scale characterization of the rock before and after each experiment using X-rays  
7 microtomography (XMT) 3D imaging.  
8 Finally, the dataset are used to establish the dependence of the  $\phi$  -  $k$  relationship on the CO<sub>2</sub>  
9 partial pressure and disequilibrium state of the fluid.

10

## 11 **2 Materials and methods**

12

### 13 **2.1 Experimental approach**

14 The experiments consisted of injecting CO<sub>2</sub>-enriched fluid through a cylindrical sample core  
15 of 9 mm diameter ( $D$ ) and 18 mm length ( $L$ ). The four percolation experiments were carried  
16 out under *in situ* sequestration conditions ( $T = 100$  °C and  $P = 12$  MPa), using various partial  
17 pressures of CO<sub>2</sub> and different ion concentrations in rock-equilibrated fluids (brine) to  
18 simulate CO<sub>2</sub>-saturated brine transport during the injection phase (Fig. 1). Table 1 presents  
19 the composition of the different fluids used in the four flow-through experiments. The  
20 geochemical code CHESS (van der Lee, 2002) was used to determine the pH of the injected  
21 CO<sub>2</sub>-enriched fluids for different fixed  $P_{\text{CO}_2}$  conditions and values of saturation index. The  
22 CO<sub>2</sub>-enriched fluid was injected at constant flow rate, corresponding to  $Q = 1.9 \times 10^{-8} \text{ m}^3 \cdot \text{s}^{-1}$   
23 for the three first experiments and  $Q = 1.0 \times 10^{-8} \text{ m}^3 \cdot \text{s}^{-1}$  for the fourth experiment. The first  
24 three experiments were performed at the same flow rate because we assumed these conditions

1 represent processes in the vicinity of the injection well, whereas experiment 4 was performed  
2 at lower flow rate to mimic flow rate far away from the injection well.

3

## 4 **2.2 The percolation apparatus**

5 A new experimental device (Fig. 2) was specifically engineered to reproduce *in situ* massive  
6 CO<sub>2</sub> injection in reservoir samples at the laboratory scale for temperatures ranging from 50 to  
7 200 °C, reservoir static pressures of 7 to 20 MPa and a partial pressure of CO<sub>2</sub> increasing up  
8 to the static pressure. Resident fluids are generally moderate to high salinity brines, almost or  
9 completely equilibrated with the rock-forming minerals prio to the CO<sub>2</sub> injection. The  
10 experimental apparatus described below allows us to study systematically the processes for  
11 any combination of these parameters.

12 The five main specific components of the device are described below: 1) a motorized dual-  
13 piston pump system that produces the flow of reservoir brine, 2) a motorized piston pump  
14 containing liquid-phase CO<sub>2</sub> cooled at 5°C, 3) the CO<sub>2</sub>-brine mixing system, 4) the  
15 percolation cell holding the sample, and 5) the back-pressure controller / sampling system  
16 (Fig. 2).

17

18 The two motorized piston pumps are equipped with displacement encoders, which allow an  
19 accurate control of the flow rate. This motorized dual pump system is operated to obtain a  
20 continuous brine flow rate ranging from  $2 \cdot 10^{-9}$  to  $2.5 \cdot 10^{-8}$  m<sup>3</sup>.s<sup>-1</sup>. The piston pump motion and  
21 the pneumatically-controlled valves are operated by a LabView-based software.

22

23 It is difficult to control the volume ratio of a two-phase fluid mixture (i.e. liquid brine and  
24 supercritical CO<sub>2</sub>). To avoid this obstacle, the mixing of the brine with CO<sub>2</sub> is carried out at  
25 high pressure (6 to 20 MPa) but low temperature (i.e. 5 °C). Under these conditions, CO<sub>2</sub> is in

1 the liquid state, which allows us to set the brine/CO<sub>2</sub> volume ratio corresponding to the  
2 desired CO<sub>2</sub> saturation of the fluid, while at the same time controlling the mixture flow rate  
3 (Fig. 3). To summarize, CO<sub>2</sub> and brine are first mixed in a cooled coil (e.g. maintained at 5  
4 °C) and then heated up to the target temperature in an oven-coated coil.

5

6 In the percolation cell, both axial and radial confining pressures are applied to the sample. To  
7 mimic natural confinement conditions, it is essential to apply a controlled confining pressure  
8 and balance the fluid injection to avoid deviatoric stresses that may damage the sample  
9 irreversibly. The axial confining pressure is applied by the axial piston, whereas the radial  
10 confining pressure is obtained by pressurization of the silicon jacket covering the sample. In  
11 our experiments, axial and radial pressures are maintained equal, at 112 % of the inlet  
12 pressure whatever its value. Therefore, we can avoid damaging the rock throughout the  
13 duration of the experiment. This system is essential to minimize stresses on the sample during  
14 pressure and temperature loading and unloading at the beginning and the end of the  
15 experiment, respectively. To achieve this objective, we make use of a pressure multiplier with  
16 a free-moving piston of dissymmetric diameter.

17

18 The minimal pressure required to avoid degassing of the CO<sub>2</sub> in the circuit is controlled by a  
19 back-pressure system that imposes a constant pressure drop whatever the flow rate. This  
20 control may become critical at low flow rates. Under such conditions, manual control is  
21 required using a micrometric valve to reduce the fluctuations to less than about 3%. These  
22 fluctuations have no impact on the permeability measurements because flow rate is in a steady  
23 state, storage is low and the pressure drop is measured continuously by a high-resolution  
24 differential pressure transducer.



1 The available flow rate ( $2.10^{-9} \leq Q \leq 2.5.10^{-8} \text{ m}^3 \cdot \text{s}^{-1}$ ) enables the exploration of a wide range  
2 of hydrodynamic conditions. Specifically, this equipment allows us to explore the entire range  
3 of fluid-rock interactions (dissolution and/or precipitation) from fully kinetically-controlled to  
4 fully transport-controlled mass transfer processes.

5

### 6 **2.3 Sample characterization**

7 The samples studied here are oolitic limestones from the Mondeville formation of Middle  
8 Jurassic age (Paris Basin). The rock is essentially composed of recrystallized ooliths with a  
9 mean diameter of less than a few hundred of  $\mu\text{m}$ , partially cemented with micritic calcite.  
10 All the samples were analysed and compared by XMT, XRD (X-Ray Diffraction), SEM  
11 (Scanning Electron Microscope) and cathodoluminescence techniques, to check that samples  
12 cored alongside each other are chemically and physically similar. Sample volumes contain  
13 thousands of pores and can be regarded as a representative elementary volume (REV) of rock  
14 (de Marsily, 1981). While heterogeneities larger than the sample size are clearly not included  
15 in this REV, the experimental results can be easily upscaled to the reservoir scale in terms of  
16 matrix properties. Cathodoluminescence and SEM analyses of the four samples show no  
17 measurable differences of chemical or structural composition. Additional analyses on whole  
18 rocks give the similar composition of the four studied samples, which corresponds to a  
19 magnesium-calcite of formula  $\text{Ca}_\alpha\text{Mg}_\beta\text{CO}_3$  with  $\alpha = 0.99$  and  $\beta = 0.01$ . The initial porosity of  
20 samples calculated from post-processing the XMT images (Noiriel et al., 2005) are similar in  
21 the case of 3 samples ( $\phi = 7.5 \pm 0.2$ ) and slightly lower ( $\phi = 6.8$ ) in the case of 1 sample.

### 22 **2.4 Monitoring changes in porosity and permeability**

23 Sample-scale changes in permeability  $k(t)$  are measured by measuring the pressure drop  $\Delta P$   
24 between the inlet and the outlet of the sample. According to Darcy's law, the ratio of the

1 volumetric flow rate  $Q$  [ $\text{m}^3 \cdot \text{s}^{-1}$ ] to the pressure difference  $\Delta P$  (Pa) scales linearly with the  
 2 sample permeability  $k$  [ $\text{m}^2$ ]:

$$3 \quad k = -\frac{\mu L Q}{S \Delta P}, \quad (1)$$

4 where  $L$  is the length of the sample in the flow direction [m],  $S$  is the cross-sectional area of  
 5 the sample [ $\text{m}^2$ ] and  $\mu$  is the dynamic viscosity of the fluid [Pa.s].

6 The fluid is collected repeatedly from the outlet port, and then analysed for  $\text{Ca}^{2+}$  and  $\text{Mg}^{2+}$   
 7 concentrations using an inductively coupled plasma-atomic emission spectrophotometer (ICP-  
 8 AES). The volume of dissolved calcite ( $V_{\text{CaCO}_3}(t)$ ) is as follows:

$$9 \quad V_{\text{CaCO}_3}(t) = Q v_{\text{CaCO}_3} \int_{\tau=0}^t \alpha \Delta C_{\text{Ca}}(\tau) + \beta \Delta C_{\text{Mg}}(\tau) d\tau, \quad (2)$$

10 where  $v_{\text{CaCO}_3}$  is the calcite molar volume ( $3.7 \times 10^{-5} \text{ m}^3 \cdot \text{mol}^{-1}$ ),  $\Delta C_{\text{Ca}}$  and  $\Delta C_{\text{Mg}}$  are the  
 11 difference of calcium and magnesium concentration respectively between the outlet and the  
 12 inlet fluids and  $\alpha$  and  $\beta$  are the fraction of Ca and Mg respectively in the calcite ( $\alpha = 99$  and  $\beta$   
 13 = 1). The sample-scale porosity  $\phi(t)$  is given by:

$$14 \quad \frac{\partial \phi(t)}{\partial t} = \frac{1}{V} \frac{\partial V_{\text{CaCO}_3}(t)}{\partial t}, \quad (3)$$

15 where  $V$  is the total sample volume (i.e.  $V = \pi L D^2 / 4$ ). To integrate equation (3), we need to  
 16 know the porosity at a given time  $t$  using, for instance, the XMT images. The procedure is  
 17 presented below in section 3.2.

18

## 19 **2.5 X-Ray Computed Micro-Tomography (XMT)**

1 Before and after each experiment, rock samples were scanned by X-ray Computed Micro-  
2 Tomography (XMT) to characterize the pore-space geometry. The XMT technique is an  
3 unmatched tool for producing nondestructive three-dimensional images of rocks without any  
4 prior preparation (Flannery et al., 1987). In the present study, data acquisition was performed  
5 at the European Synchrotron Radiation Facility (ESRF) in Grenoble (France) using the ID19  
6 beam-line. The principle of XMT is based on the 3D computed reconstruction of an object  
7 partially absorbent to X-rays, using a set of 2D detector readings acquired at different angular  
8 positions. A total of 1 500 x-ray readings were recorded, using an exposure time of 2 s at each  
9 angle and a rotational interval of 0.12 degree along the core axis (Fig. 4).

10 For each X-ray reading, the monochromatic X-ray beam passes through the sample and then  
11 reaches the scintillator, which converts it into visible light recorded by a high-speed digital  
12 CCD camera ( $2048 \times 2048$  pixels). The pixel resolution is  $5.06 \mu\text{m}$ , which is a function of the  
13 optical bench setup. Synchrotron radiation provides several advantages over conventional X-  
14 ray sources, including the production of a homogeneous, parallel, monochromatic and highly  
15 coherent photon flux. This results in high-quality images having a resolution of about the size  
16 of the voxel dimension. For a given energy of incident X-ray beam (here 40 keV), the  
17 attenuation depends on the chemical composition of the rock, specifically, the atomic number  
18 of its components and their mass fraction per volume (i.e. the density). In mono-crystalline  
19 rocks such as the samples studied here, XMT images yield the distribution of densities in the  
20 rock, or in other words, 3D porosity maps.

### 21 **3. Experimental results and discussion**

22 Changes of permeability and porosity in porous media are attributed to dissolution and  
23 precipitation. These dynamic processes are constrained from concurrent measurements of  
24 evolving permeability, mineral mass flux and sample pore structure. Because of the non-

1 destructive nature of XMT imaging, we can also observe the progression of the chemical  
 2 reaction over the porous sample as well as related morphological changes.

### 3 **3.1. Mass transfers during reaction**

4 Fig. 5 reports the normalized time-resolved Ca and Mg concentration

5  $\Delta C_i(t) = C_i(t)|_{out} - C_i(t)|_{in}$  with  $i = \text{Ca}$  and  $\text{Mg}$ , for the four experiments denoted D1, D2,

6 D3 and P1. By convention, we define  $t = 0$  when the  $\text{CO}_2$  pump is activated. Experiments D1,

7 D2, D3 and P1 are set up to mimic mass transfers at the locations 1, 2, 3 and 4 shown in Fig.

8 1 respectively.

#### 9 **Dissolution experiments D1 - D3**

10 The ratio  $\Delta C_{Ca}(t)$  to  $\Delta C_{Mg}(t)$  is roughly 99, which corresponds to the Ca/Mg mole fraction

11 ratio of the whole rock, i.e. a magnesium-calcite of formula  $\text{Ca}_{0.99}\text{Mg}_{0.01}\text{CO}_3$ .  $\Delta C_{Ca}(t)$  and

12  $\Delta C_{Mg}(t)$  display similar trends indicating congruent dissolution of the rock (Fig. 5). From

13 this point, we describe processes using  $\Delta C_{Ca}(t)$  data alone, but in the calculations, such as

14 for porosity (equations 2 and 3), we account for the Ca/Mg stoichiometry of the rock-forming

15 calcite. For D1, D2 and D3, the initial increase of  $\Delta C_{Ca}$  (for  $t < \tau_0$  with  $\tau_0 \leq 20$  minutes)

16 reflects the dispersion of the  $\text{CO}_2$  front in the circuit and transient processes in the sample.

17 Indeed, for  $t < \tau_0$ ,  $\partial_t C_{Ca}|_{out} > 0$  (with  $\partial_t(\cdot)$  denoting the time derivative).

18 For  $t \geq \tau_0$ ,  $\Delta C_{Ca}$  decreases and tends to an asymptotic value at  $t = \tau_e$ , for example when

19  $\tau_e \approx 90$  minutes as in the case of D2. The period of decreasing  $\Delta C_{Ca}$ , for  $\tau_0 < t < \tau_e$ ,

20 corresponds to preferential dissolution of the cement and oolite roughness microstructures

21 starting at the inlet and progressing to the outlet (Fig. 6). Then, when the cement is dissolved,

22 the calcium flux at the outlet is linked to dissolution of the oolitic fraction, which appears to

23 be almost stationary. The distinctly different dissolution regimes for D1, D2, and D3 are

1 characterized by the value of  $\partial_t(\Delta C_{Ca})$  for  $t < \tau_e$ , the asymptotic value of  $C_{Ca}|_{out}$  for  
 2  $t \geq \tau_e$  and the value of  $\tau_e$  (Fig.5). The attainment of an asymptotic value corresponds to the  
 3 occurrence of sample-averaged steady-state mass transfer.

4 Experiments D1, D2 and D3 display dissolution processes, i.e.  $\Delta C_{Ca}(t) > 0$ . Assuming that  
 5 the Mg content of the rock is negligible, the dissolution reaction is predominantly



7 with the equilibrium constant  $K(T = 100^\circ\text{C}) = a_{Ca} a_{\text{HCO}_3^-} / a_{\text{H}} = 0.168$ , where  $a_i = \gamma_i C_i$  denotes  
 8 the activity of species  $i$  with activity coefficient  $\gamma_i$  evaluated using the modified Debye-  
 9 Huckel formulation for ionic strengths up to at least 2 mol.L<sup>-1</sup> (Bethke, 1996). The outlet  
 10 concentrations  $C_{Ca}(t)|_{out}$  and  $C_{Mg}(t)|_{out}$  are always lower than the equilibrium concentrations  
 11  $\tilde{C}_{Ca}$  and  $\tilde{C}_{Mg}$ , respectively, highlighting the kinetic control of the dissolution reaction. Using  
 12 the transition state theory (Lasaga, 1998), the instantaneous sample-scale effective reaction  
 13 rate [mol.m<sup>-3</sup>.s<sup>-1</sup>] for calcite dissolution (equation 4) can be written as:

$$14 \quad R_{eff} = \frac{r S_r (1 - \langle I \rangle)}{\phi V}, \quad (5)$$

15 where the kinetics coefficient  $r$  is an intrinsic property of the reaction for a given pH profile  
 16 (Lasaga, 1998) [mol.m<sup>-2</sup>.s<sup>-1</sup>],  $S_r$  is the reaction surface area of the sample and  $\langle I \rangle$  is the  
 17 sample-averaged saturation index. For  $t \geq \tau_e$ , this index is approximated by

18  $\langle I \rangle = [I_{out} + I_{in}] / 2$ . The saturation index for calcite in the outlet fluid is given by

$$19 \quad I_{out} = \frac{IAP}{K_{eq}} = \frac{a_{Ca^{2+}}|_{out} a_{\text{HCO}_3^-}|_{out}}{a_{\text{H}^+}|_{out} K_{eq}}, \quad (6)$$

1 where IAP stands for the Ion Activity Product of the outlet fluid at time  $t \geq \tau_e$ . The value of  
 2  $I_{out}$  is 0.22 for D1, 0.28 for D2 and 0.60 for D3, whereas the saturation index for the inlet  
 3 fluid, calculated by replacing the outlet fluid concentration by the inlet fluid concentration in  
 4 equation (6), is  $1.9 \times 10^{-4}$  for D1,  $5.3 \times 10^{-4}$  for D2 and  $22.9 \times 10^{-4}$  for D3.

5 The experiments presented here clearly show the role of CO<sub>2</sub> partial pressure in driving the  
 6 dissolution process. As described by Golfier et al. (2002), the dissolution mechanism, at the  
 7 pore-scale, can be separated into three steps: i) transport (by diffusion and advection) of the  
 8 reactants to the reaction surface, ii) heterogeneous reaction at the surface (i.e. surface  
 9 reaction), and iii) transport of reaction products away from the surface. The effective kinetics  
 10 is controlled by the slowest of these three steps. It is generally accepted that transport of the  
 11 solute to and from the reactive surface is associated with similar characteristic times. Thus,  
 12 we can consider two limit cases. If the characteristic time of reaction is short compared to the  
 13 characteristic time of transport, the reaction is called transport-limited. Conversely, if the  
 14 hydrodynamic renewal of the reactive fluid is high, then the reaction is reaction-rate-limited.  
 15 This behaviour is characterized macroscopically by the sample-scale Damköhler number,

$$16 \quad Da \equiv \frac{\langle \bar{\gamma} \rangle l}{\langle \bar{u} \rangle}, \quad \text{for } Pe \gg 1, \quad (7)$$

17 where  $\langle \bar{\gamma} \rangle$  is the sample-averaged reaction rate [ $s^{-1}$ ],  $l$  is the pore length [m],  $\langle \bar{u} \rangle$  is the  
 18 sample-averaged seepage velocity magnitude [ $m \cdot s^{-1}$ ] and  $Pe \equiv \langle \bar{u} \rangle l / d_0$  is the local Peclet  
 19 number that characterise reactant renewing at the fluid-rock interface, with  $d_0$  the molecular  
 20 diffusion ( $7.5 \times 10^{-10} \text{ m}^2 \cdot s^{-1}$  for Ca). Values of  $Pe$  are larger than  $10^2$  for experiments D1 to  
 21 D3, so that the  $Pe$  condition for equation (7) is satisfied.

22 If  $Da < 1$ , dissolution is reaction-rate-limited, whereas dissolution is transport-limited if  
 23  $Da > 1$ . At the Darcy scale, with  $Pe \gg 1$ , transport-limited dissolution will lead to non-

1 uniform dissolution. The localization of dissolution features is a result of positive feedback  
 2 between the local increase of pore diameter and the renewal capacity of the fluid in these  
 3 enlarged pores (Hoefner and Fogler, 1988; Golfier et al., 2002). In this case, we would expect  
 4 the formation of highly conductive flow channels, known as wormholes. The distribution and  
 5 shape of the wormholes are controlled by the (initial) heterogeneity of the pore structure and  
 6 the correlation length of the (initial) permeability field. For the value of  $Pe$  encountered here,  
 7 we expect the properties of the wormholes to be independent of  $Pe$  because the diffusive  
 8 transport is negligible.

9 Using equation (5), the sample-averaged reaction rate  $\langle \bar{\gamma} \rangle$  is

$$10 \quad \langle \bar{\gamma} \rangle = \frac{r S_r (1 - \langle I \rangle)}{\langle \phi \rangle V (\Delta C_{Ca})^*}, \quad (8)$$

11 where  $(\Delta C_{Ca})^*$  is the asymptotical, *i.e.* for  $t \gg \tau_e$ , calcium mass balance in the sample (*i.e.*  
 12  $C_{Ca}|_{out} - C_{Ca}|_{in}$ ) for  $Da = 1$ . Note that  $\langle I \rangle$ ,  $\langle \phi \rangle$  and  $S_r$  are time dependent. Conversely, the  
 13 instantaneous Ca asymptotical mass balance in the sample, for  $Da \neq 1$ , is

$$14 \quad C_{Ca}|_{out} \approx C_{Ca}|_{in} + \frac{r S_r (1 - \langle I \rangle)}{Q}. \quad (9)$$

15 Note that the Ca concentration at the outlet is independent on the initial porosity. Combining  
 16 equations (7) to (9), we obtain the expression of the Damköhler number as a function of the Ca  
 17 concentration balance alone:

$$18 \quad Da = \frac{(\Delta C_{Ca})}{(\Delta C_{Ca})^*}. \quad (10)$$

19 By definition,  $Da < 1$  denotes a reaction-rate-limited behaviour that we assume reflects  
 20 homogeneous dissolution in the sample. While such is the case for D3 (Fig. 7 and 8), we  
 21 observe significant wormhole structures for D2. Consequently, the value of  $(\Delta C_{Ca})^*$  is  
 22 evidently close to the value of  $C_{Ca}|_{out} - C_{Ca}|_{in}$  measured for D3. In the following, we assume

1 that  $(\Delta C_{Ca})^*$  is equal to  $C_{Ca}|_{out} - C_{Ca}|_{in}$  measured for D3 at  $t \geq \tau_e$ . Hence,  $Da = 7.5$  for D1  
 2 and  $Da = 3.1$  for D2, corresponding to transport-limited dissolution. The expected patterns  
 3 of dissolution localization are confirmed by the XMT images obtained for experiments D1  
 4 and D2 (Fig. 7 and 8). Clearly, the properties of the wormholes are controlled by the  
 5 composition of the fluid. For experiment D1, we observe the formation of several conical  
 6 penetrative wormholes as described by Golfier et al. (2002). Experiment D2 displays a more  
 7 diffuse pattern of wormholes.

8

### 9 **Precipitation**

10 For experiment P1, fluid analysis shows that  $\Delta C_{Ca} \approx 0$  and  $\Delta C_{Mg} < 0$  whatever the value of  $t$ .  
 11 Precipitation is likely associated with either magnesite precipitation or dolomitization of the  
 12 calcite. The value of  $C_{Mg}|_{out}$  decreases by 47% for  $t < t_e$ , with  $t_e \approx 600$  minutes, then  
 13 stabilizes at around  $0.98 \times 10^{-3} \text{ mol.L}^{-1}$  for  $t \geq t_e$ . SEM imaging coupled with chemical  
 14 analysis yields a magnesium-calcite of formula  $\text{Ca}_\alpha\text{Mg}_\beta\text{CO}_3$  with  $\alpha = 0.88-0.96$  and  $\beta = 0.04-$   
 15  $0.12$  localized at the ooloth surfaces (Fig. 9). Consequently, the dominant process is  
 16 dolomitization.

17

### 18 **3.2. Porosity and permeability changes**

19 As stated in section 2.4, we require a reference value of the porosity to calculate the porosity  
 20 by integration of equation (3). Porosity measured by processing the XMT data (Noiriel et al.,  
 21 2005) is expected to be misevaluated because of the cutoff scale imposed by the voxel size  
 22 dimension. Indeed, the surface roughness and microstructures of the micritic cement are not  
 23 properly resolved because they are on a smaller scale than the XMT resolution (i.e.  $5.06 \mu\text{m}$ ).  
 24 Nevertheless, both the cements and ooloth roughness microstructures display large reactive



1 surface-areas and are dissolved in the early stage of the experiments (i.e.  $t < \tau_e$ ). For each of  
 2 the dissolution experiments, the porosity measured by XMT at the end of the experiment is  
 3 the best evaluation of the true porosity. Consequently, using equation (3), we can write the  
 4 sample-averaged porosity for a given experiment as follows:

$$5 \quad \phi(t) = \phi^* - \frac{(V_{CaCO_3})^* - V_{CaCO_3}(t)}{V}, \quad (11)$$

6 where  $\phi^*$  and  $(V_{CaCO_3})^*$  are the porosities obtained by XMT and the volume of dissolved  
 7 calcite at the end of the experiment, respectively. In the case of experiment P1, the reference  
 8 porosity is taken at  $t = 0$ . Equation (11) can then be rewritten as

$$9 \quad \phi(t) = \phi^{(0)} + (V_{CaCO_3}(t) - (V_{CaCO_3})^{(0)})/V \text{ in this case. Consequently, we expect a higher}$$

10 uncertainty on the value of the initial porosity  $\phi^{(0)}$ . Fig. 10 presents the sample-averaged  
 11 change in porosity for the four experiments (D1, D2, D3 and P1). For  $\tau_0 < t < \tau_e$ , the porosity  
 12 trends,  $\phi(t)$ , display a pre-asymptotic decrease corresponding to dissolution of the smaller  
 13 structures (e.g. cements) in experiments D1 to D3. This pre-asymptotic decrease reflects the  
 14 migration of the dissolution front from the inlet to the outlet of the sample. Then, for  $t \geq \tau_e$ ,  
 15 the dissolution rate ( $\partial_t \phi$ ) tends to a constant value, while dissolution of the oolith surface  
 16 becomes homogeneous. Similar results were obtained by Gouze et al. (2003) for the  
 17 dissolution of initially rough-walled fractures in carbonate, as well as by Noiriél et al. (2004)  
 18 for the dissolution of a porous limestone sample at low temperature. This behaviour is more  
 19 marked in experiments D1 and D2, where dissolution is initially concentrated in the vicinity  
 20 of the inlet as shown in Fig. 7. The values of  $\partial_t \phi$ ,  $\forall t$ , are higher for experiment D1 and  
 21 lower for experiments D2 and D3, highlighting the higher reactivity of the fluids at higher  
 22  $P_{CO_2}$ .

1 In the precipitation experiment (P1), we observe a steady decrease in porosity during the 700  
 2 minutes run time. Precipitation features cannot be visualized by the XMT technique, because  
 3 they are smaller than the XMT resolution (5.06  $\mu\text{m}$ ).  
 4 Fig. 11 shows the corresponding changes in permeability with time  $k(t)$ . We derive a  
 5 measure of  $k(t)$  from the differential pressure records using equation (1) with a constant flow  
 6 rate. As expected, permeability increases in the three dissolution experiments (D1 - D3),  
 7 whereas it decreases in the precipitation experiment (P1). We should point out that the  
 8 samples used for the three dissolution experiments are similar, with an initial permeability of  
 9 around  $35 \times 10^{-15} \text{ m}^2$ , while the sample used in experiment P1 has a higher initial permeability  
 10 (i.e.  $180 \times 10^{-15} \text{ m}^2$ ), even all samples were taken side-by-side from the same core.  
 11 Permeability changes are clearly linked to the  $P_{\text{CO}_2}$  value as well as the Ca concentration in the  
 12 inlet fluid. Experiments D1 and D2 display well-marked dual slope permeability trends  
 13 corresponding to the dissolution regime change at  $t = \tau_e$ . The rate of increase in permeability,  
 14  $\partial_t k$ , is almost stationary for experiment D3, which, conversely, displays uniform dissolution  
 15 behaviour. For experiment P1,  $k(t)$  is characterized by two distinctly different rates, which  
 16 are nevertheless associated with a single rate of decrease in porosity (Fig. 10). The origin of  
 17 this behaviour is discussed in the next section.

18

### 19 **3.3. Determination of $Da$ -controlled $\partial k / \partial \phi$ laws**

20 The distinctly different porosity and permeability trends obtained in experiments D1 – D3  
 21 characterize dissolution patterns controlled by initial  $\text{CO}_2$  partial pressure and calcite  
 22 saturation index. We should bear in mind that the saturation index depends on Ca  
 23 concentration alone, because all the other parameters are constant and the rock samples are  
 24 identical. Up to this point in the discussion, our results show that dissolution can display

1 distinctly different patterns along the path followed by CO<sub>2</sub>-enriched fluids in the reservoir.  
 2 However, we cannot use this observation to model reservoir-scale processes until both the  
 3 porosity changes and the related permeability changes are parameterized according to the  
 4 fluid composition. Hence, our objective is to establish a relation between the measured  
 5 sample-scale porosity-permeability relationship and the value of  $Da$ .  
 6 Permeability is an intrinsic macroscopic property of the rock that results from a combination  
 7 of several parameters including the geometry of the pores and throats, as well as, more  
 8 importantly, the sample-scale connectivity of the voids (Mavko and Nur, 1997; Pape et al.  
 9 1999). In spite of this complexity, the essential behaviour can often be evaluated successfully  
 10 from the porosity  $\phi$  using power-law relationships such as the Kozeny-Carman model  
 11 (Kozeny, 1927; Carman, 1937):  $k \equiv \lambda \phi^n / S^m$ , where  $S$  is the specific surface-area, and  $\lambda$  is a  
 12 geometric factor expressing all the other rock-specific static parameters, while  $n$  and  $m$  reflect  
 13 the dynamic behaviour of the relation. For example, the values of  $n$  and  $m$  for homogeneous  
 14 sandstones (e.g. Fontainebleau sandstones) are close to 3 and 2, respectively (Bernabé et al.,  
 15 2003). Evidently, in the case of rocks displaying complex pore structures, such as low-  
 16 porosity carbonate rocks, the specific surface-area is not measurable and is certainly not the  
 17 main parameter controlling permeability. Several alternative relations have been proposed to  
 18 account for deviations from the Kozeny-Carman model. In instance, Bourbié et al. (1987)  
 19 proposed the scaling relation  $k \equiv \lambda' \phi^n d^2$ , where  $d$  is the grain diameter. However, it is not  
 20 easy to measure the grain diameter in most limestone rocks because of the large granulometric  
 21 variability and marked anisotropy of the “grain” shape. For low-porosity media, it is often  
 22 observed that changes in permeability scale with porosity only if  $k \sim \phi^n$  for a given rock type  
 23 (Bernabé et al., 1982). The simplest relationship is

$$24 \quad k \equiv \theta(\phi - \phi_c)^n, \quad (12)$$

1 where the unit scaling and constant parameters characterizing the rock and the mass transfer  
 2 processes are lumped together in  $\theta$  and  $n$ , respectively. In equation (12),  $\phi_c$  is the value of  
 3 porosity at the percolation threshold ( $k = 0$  if  $\phi = \phi_c$ ). A similar power-law relationship was  
 4 used by Noiriél et al. (2004) to account for the course of limestone dissolution. These authors  
 5 (*op.cit.*) show that this relation gives rise to an asymptotic trend under conditions of  
 6 dominantly homogeneous dissolution. However, while also being considered as independent  
 7 of porosity, the value of  $\theta$  is valid for a specific range of porosity that must be defined  
 8 experimentally.

9 Figure 12 shows the evolution of permeability versus porosity during experiment P1. We note  
 10 that P1 is characterized by dolomitization of the oolite surfaces, with both  $\phi$  and  $k$   
 11 decreasing. The plot of  $\log(\phi)$  vs.  $\log(k)$  reveals two trends with a transitional behaviour  
 12 between  $t = t_p = 400$  min and  $t = t_e = 600$  min. In the first part of the experiment, for  
 13  $t < t_p$ , the  $\log(\phi)$  vs.  $\log(k)$  plot is linear and equation (8) can be applied with a very low  
 14 value of the power law exponent:  $n = 0.18$ . Conversely, for  $t > t_e$ ,  $\log(\phi)$  vs.  $\log(k)$  is not  
 15 linear, i.e.  $\partial(\log(k))/\partial(\log(\phi)) > 0$ . This indicates that porosity approaches the percolation  
 16 threshold  $\phi_c$ . We use a polynomial approximation to evaluate  $\phi_c \approx 0.059$ .

17  
 18 Fig. 13 shows the variation of permeability as a function of porosity during the dissolution  
 19 experiments D1 – D3. For experiment D1, the variation of  $\log(\phi)$  vs.  $\log(k)$  displays a dual  
 20 slope behaviour reflecting the dual dissolution regime illustrated by the porosity profile in  
 21 Fig. 7. It is difficult to interpret the value of  $n = 0.79$  obtained when  $\tau_0 < t < \tau_e$  because  
 22 this result reflects both the low increase in permeability in the outlet side of the sample and  
 23 the high increase in porosity near the inlet. For this experiment, the useful part of the  $\log(\phi)$

1 vs.  $\log(k)$  plot is the segment characterizing the stationary dissolution process, i.e.  $t > \tau_e$ , i.e.  
2 when the value of  $n_{(D1)} = 4.79$ .

3 For experiment D2 and D3, we obtain a single-slope  $\log(\phi)$  vs.  $\log(k)$  plot for  $t > \tau_0$  with  
4  $n_{(D2)} = 1.24$  and  $n_{(D3)} = 0.29$ , respectively. This result is somewhat surprising because it  
5 implies that the change in permeability with porosity can be described as a single  
6 phenomenological process, while the rate of calcium production  $\partial_t C_{Ca}|_{out}$  is not stationary  
7 for  $\tau_0 < t < \tau_e$ . Physically, this means that, when a high rate of dissolution is associated with  
8 high  $S_r$  for cements and oolite rough surfaces, the slope (i.e.  $\partial k / \partial \phi$ ) obtained for  
9  $\tau_0 < t < \tau_e$  is identical to the slope for  $t > \tau_e$ , when the dissolution rate is slower because of  
10 the lower value of  $S_r$ . In other words, for a given volume of dissolved calcite, dissolving  
11 cements and oolite surface roughness is less efficient in terms of increasing the permeability  
12 than dissolving massive oolites. This behaviour is probably linked to the hydro-chemical  
13 history of the specific rock studied here, which displays high permeability ( $35 \times 10^{-15} \text{ m}^2$ ) and  
14 low porosity. Indeed, this sequence from the Middle Jurassic of the Paris Basin corresponds to  
15 an aquifer with considerable flow of fluids having a composition very close to equilibrium  
16 (Coudrain and Gouze, 1993). Thus, we can assume that the slow redistribution of mass over  
17 several million years has acted to minimize the hydraulic energy loss. Consequently, these  
18 slow processes lead to a redistribution of micritic phases into zones where fluid flow is slow  
19 (i.e. in pore voids), while strategic flowpaths such as pore throats remain free of micritic  
20 growths. These features can be seen from microscope observations of the rock thin-sections.

21 The  $k - \phi$  relationships are clearly linked to fluid chemistry for  $Pe \gg 1$ ; under this  
22 condition,  $n$  increases with  $Da$ . Consequently, the parameterization of the  $k - \phi$  power law  
23 is required for predictive reservoir (Darcy scale) modelling. In large-scale meshed-reservoir

1 simulators, the local averaged  $Da$  (equation 10) can be easily calculated from the local  
 2 (nodal) values of reactant concentration in the fluid. Fig. 14 shows the relationship between  $n$   
 3 and  $Da$ , which appears to be scaled according to a power law:  $n = A + B Da^C$ , where  $A + B$   
 4 gives the value of  $n$  for  $Da = 1$ , i.e.  $n = 0.29$ , and  $C$  is the scaling exponent. The best fit is

$$5 \quad n = 0.10 + 0.18 Da^{1.60} \quad (13)$$

6 Note that the value of  $C$  is independent of the uncertainties associated with the definition of  
 7  $(\Delta C_{Ca})^*$  (see equation 10), while the value of  $B$  is controlled by the value of  $n$  for  $Da = 1$ . A  
 8 better evaluation of  $B$  would require performing experiments with  $P_{CO_2}$  ranging between the  
 9 conditions used for experiments D2 and D3. Conversely, the value of  $A$  is independent of the  
 10 uncertainties associated with the definition of  $(\Delta C_{Ca})^*$ , provided the value of  $n$  measured for  
 11 experiment D3 is indeed the lower value associated with  $Da = 1$ . This can be checked by  
 12 performing an experiment with  $P_{CO_2}$  lower than the value used for experiment D3.

#### 13 **4. Conclusion**

14 We present a set of four flow-through experiments allowing us to describe mass transfer  
 15 processes (1) in the vicinity of the injection well where  $P_{CO_2}$  is maximal and dissolution is  
 16 non-uniform, and (2) at distant locations where dissolution becomes more and more uniform,  
 17 up to a point where precipitation (calcite dolomitization) is observed. This set of experiments  
 18 is performed for  $P - T - P_{CO_2}$  conditions representative of the most probable *in situ* conditions.

19

20 As a general rule, we expect non-uniform dissolution to occur near the injection well in  
 21 calcite-rich reservoirs because of the high reactivity of calcite at low pH conditions. The  
 22 experiment performed with  $P_{CO_2}$  close to the total pressure  $P$  supports the formation of highly  
 23 conductive long-distance correlated flow channels, indicating transport-controlled dissolution.

1 These features strongly modify the permeability, while the macroscopic porosity is only  
 2 moderately affected. For intermediate values of  $P_{CO_2}$ , the mass transfer changes from  
 3 transport-controlled to kinetically-controlled dissolution. Uniform dissolution is obtained for  
 4  $P_{CO_2} = 2.5$  MPa. These three dissolution experiments display distinctly different scaling laws  
 5 relating the variations of porosity against permeability. Clearly, classical laws relating  
 6 permeability ( $k$ ) to porosity ( $\phi$ ) using rock-dependent parameterization alone cannot account  
 7 for changes in permeability triggered by local fluid-rock disequilibrium. Hence, macroscale  
 8 porosity-permeability relationships must be parameterized not only to reflect the rock-type-  
 9 dependent properties, as generally performed when modelling low-reactivity systems, but also  
 10 to take account of the local dissolution regime.

11 Finally, for the experiment with  $P_{CO_2} = 0.7$ , i.e. reproducing conditions far from the injection  
 12 well, we observe a uniform decrease of the porosity associated with dolomitization of the  
 13 reservoir. However, the rate of decrease in permeability rises sharply as the porosity  
 14 approaches  $\phi_c$ , indicating a probable clogging of the medium if dolomitization conditions  
 15 persist.

16 Using this set of experiments, we extract step by step the macroscopic parameters required to  
 17 formulate the dependence of the porosity-permeability scaling on local fluid-rock  
 18 disequilibrium:

- 19 1) The value of porosity at the percolation threshold is evaluated using the precipitation  
 20 experiment ( $P_{CO_2} = 0.7$ ),
- 21 2) The sample-scale threshold value of the Damkolher number ( $Da = 1$ ) is defined from  
 22 the uniform dissolution experiment ( $P_{CO_2} = 2.5$ ),

- 1        3) The value of  $Da$  for each of the non-uniform dissolution experiments (i.e. with  $P_{CO_2} =$   
2        6.0 and 10 MPa) is calculated from the amount of calcium produced in the sample,
- 3        4) The exponent  $n$  of the porosity-permeability power law in the relation  $k \sim (\phi - \phi_c)^n$  is  
4        measured from the asymptotic dissolution regime for each of the experiments,
- 5        5) The relationship  $n$  versus  $Da$  is fitted to produce a macroscopic phenomenological law  
6        that can be upscaled easily to be implemented in classical reservoir numerical  
7        simulators.

8        Interestingly, we find that the relation between  $n$  and  $Da$  is a power law similar to the  
9        porosity-permeability scaling relationship. Evidently, the coefficients of this law are (highly)  
10       dependent on the properties of the reservoir and must be measured case by case. The new  
11       experimental apparatus and procedure described here probably represent the best approach to  
12       measure these parameters.

13       It is beyond the scope of our study to calculate systematically the errors generated by  
14       adopting a porosity-permeability scaling law that is independent of the local chemical  
15       disequilibrium, even though such an approach is commonly used in modelling. However, in  
16       view of the large value ( $C = 1.6$ ) of the exponent in the power law scaling relation  $n \sim Da^C$ ,  
17       any errors produced by assuming a constant value of  $n$  would clearly jeopardize the  
18       assessment of risks associated with the injection and long-term underground storage of  $CO_2$   
19       in limestones.

20

21

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- 33

1 **Figure captions**

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4 **Fig. 1:** Schematic illustration of a CO<sub>2</sub> storage facility in a sedimentary reservoir. Boxes 1 to  
5 4 represent the decrease of CO<sub>2</sub> partial pressure along fluid transfer pathways into a host  
6 reservoir. For our experiments, in box 1:  $P_{CO_2} = 100$  bar (D1), box 2:  $P_{CO_2} = 60$  bar (D2), box  
7 3:  $P_{CO_2} = 25$  bar (D3) and box 4:  $P_{CO_2} = 7$  bar (P1).

8

9 **Fig. 2:** Diagram of the experimental setup.

10

11 **Fig. 3:**  $P - T$  phase diagram for CO<sub>2</sub>, with P-T path corresponding to CO<sub>2</sub>-brine mixing.

12

13 **Fig. 4:** Sketch diagram of the X-ray microtomography acquisition line.

14

15 **Fig. 5:** Normalized time-resolved concentrations of  $Ca$  (on right) and  $Mg$  (on left). Results are  
16 presented for each experiment, D1 (circles), D2 (squares), D3 (diamonds) and P1 (crosses).  
17 Note that the time scale for the dissolution experiment is not the same as for the precipitation  
18 experiment.

19

20 **Fig. 6:** XMT cross-section of the sample used for experiment D1. Left column shows the X-  
21 ray images before and after the dissolution experiment. Grey levels indicate the X-ray  
22 absorption intensity. Middle column shows the corresponding binary images, with calcite  
23 indicated in white and voids in black. Dissolved calcite (in white) is visualized on the right  
24 hand figure.

25

26 **Fig. 7:**  $x$ - $y$  averaged porosity profiles along the samples in the flow direction ( $z$ ) before the  
27 experiment (dotted) and after the experiment (plain).

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29 **Fig. 8:** 3D XMT images of the cores before (top line) and after (bottom line) for experiments  
30 D1, D2 and D3. Black and white areas represent voids and solids, respectively. Image  
31 dimensions are: diameter 9 mm and height 4.5 mm.

32

33 **Fig. 9:** Secondary electron micrographs (SEM) showing dolomite precipitated during  
34 experiment P1.

35

36 **Fig. 10:** Variation of porosity with elapsed time; D1 (circles), D2 (squares), D3 (diamonds)  
37 and P1 (crosses).

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39 **Fig. 11:** Variation of sample permeability with elapsed time for the dissolution experiments  
40 (D1 – D3) and the precipitation experiment P1.

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42 **Fig. 12:** Log permeability versus log porosity for the precipitation experiments.

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44 **Fig. 13:** Log permeability versus log porosity for the dissolution experiments D1 (circles), D2  
45 (squares) and D3 (diamonds).

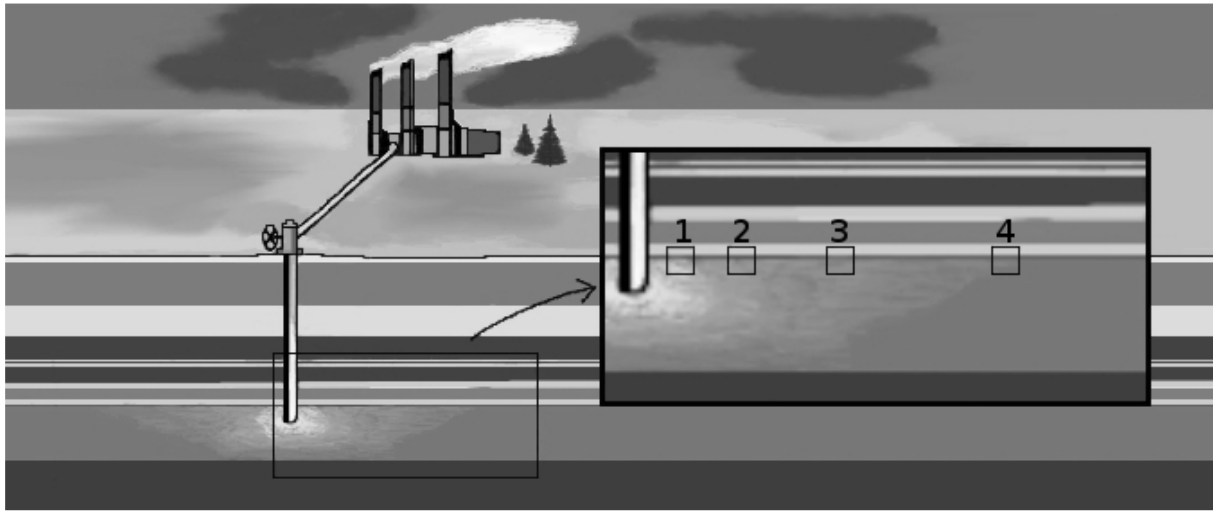
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47 **Fig. 14:** Scaling exponent  $n$  versus value of the Damkolher number  $Da$  for the dissolution  
48 experiments D1 – D3. The regression coefficient  $R$  is optimal ( $R^2 = 1$ ).

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Species (mg.L <sup>-1</sup> )	D1	D2	D3	P1
Na	23 000	23 000	23 000	23 000
Ca	330	375	400	3500
Mg	4	4.5	5	45
Cl	35 000	35 000	35 000	35 000
CO <sub>2</sub> (mol.L <sup>-1</sup> )	0.8	0.5	0.2	0.06
pH	3.21	3.51	4.02	8.7

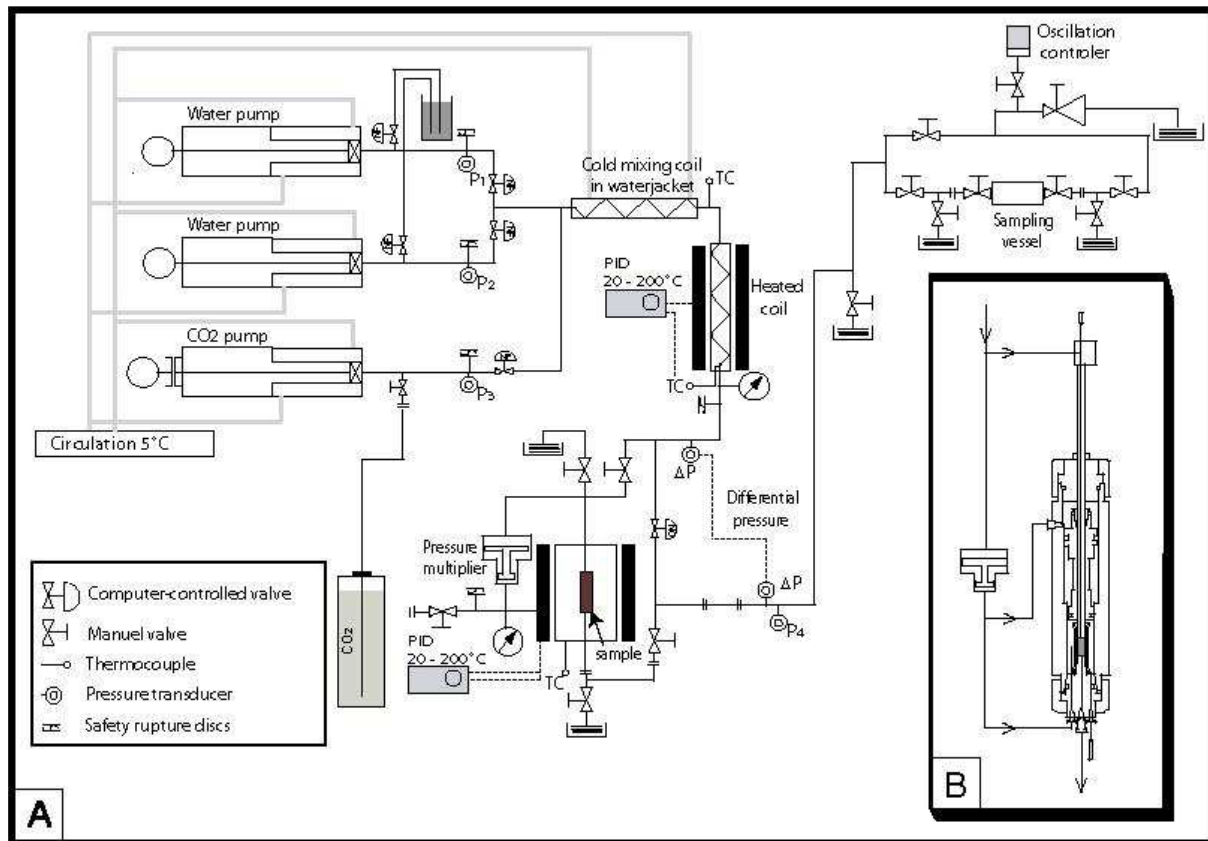
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7**Table 1:** Composition of fluids for experiments D1, D2, D3 and P1 (in mg.L<sup>-1</sup>).



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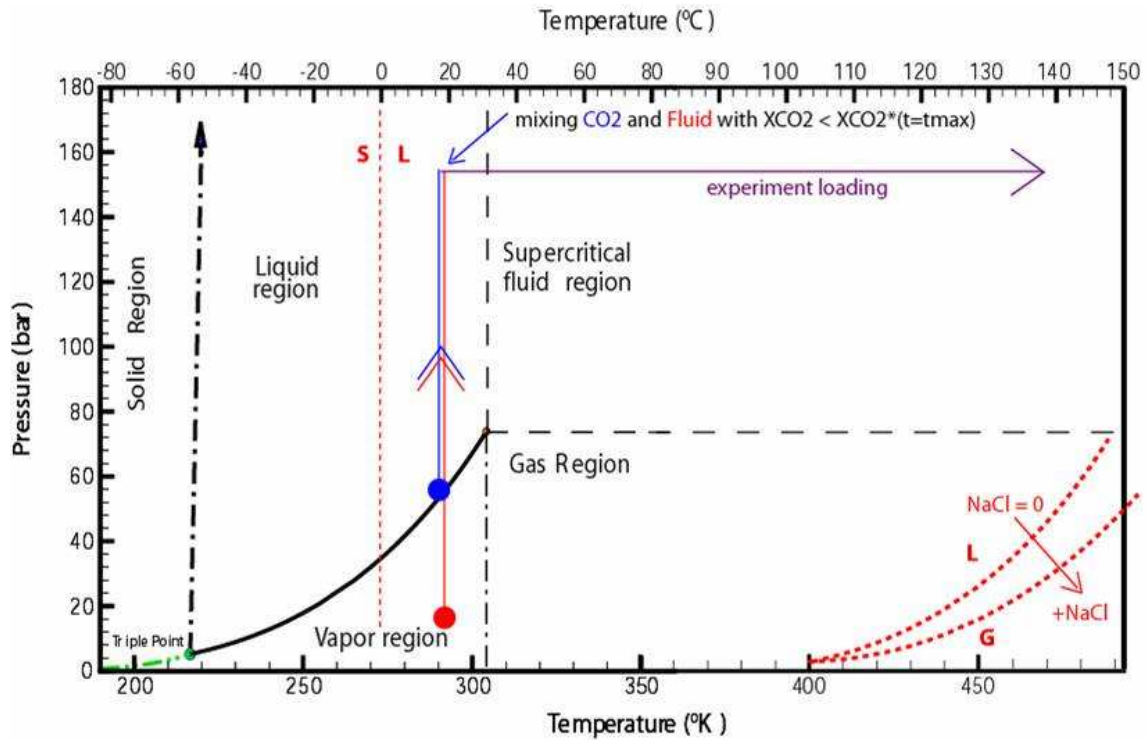


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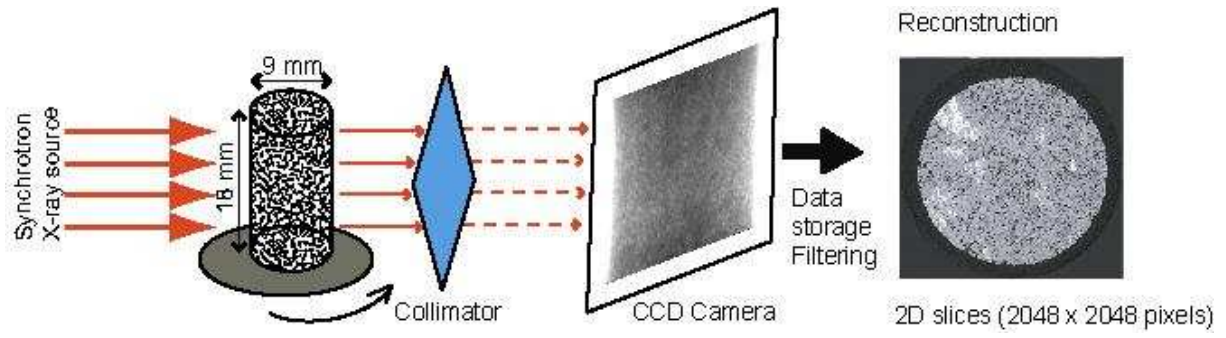
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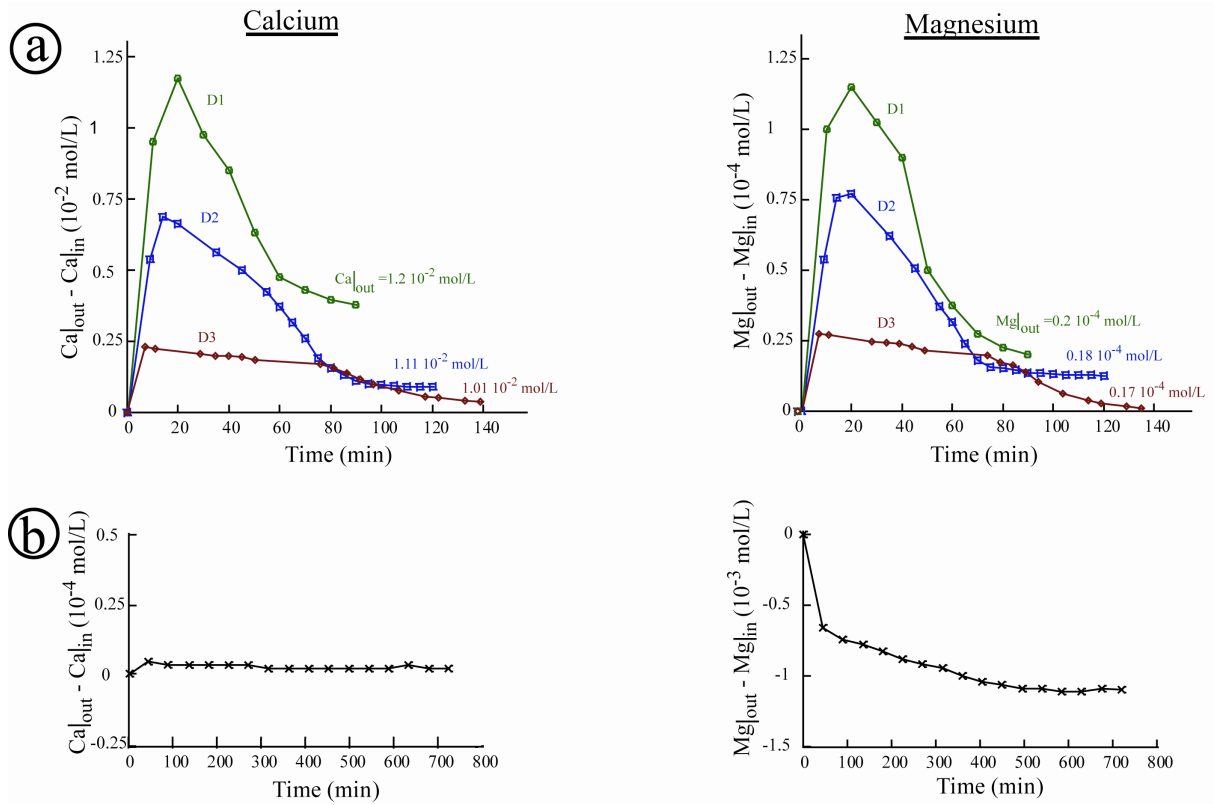
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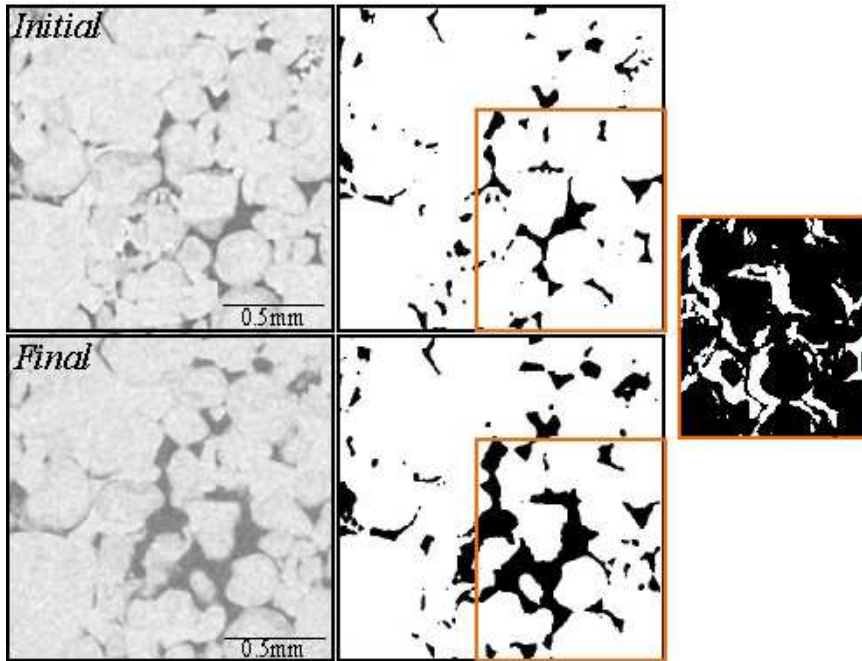
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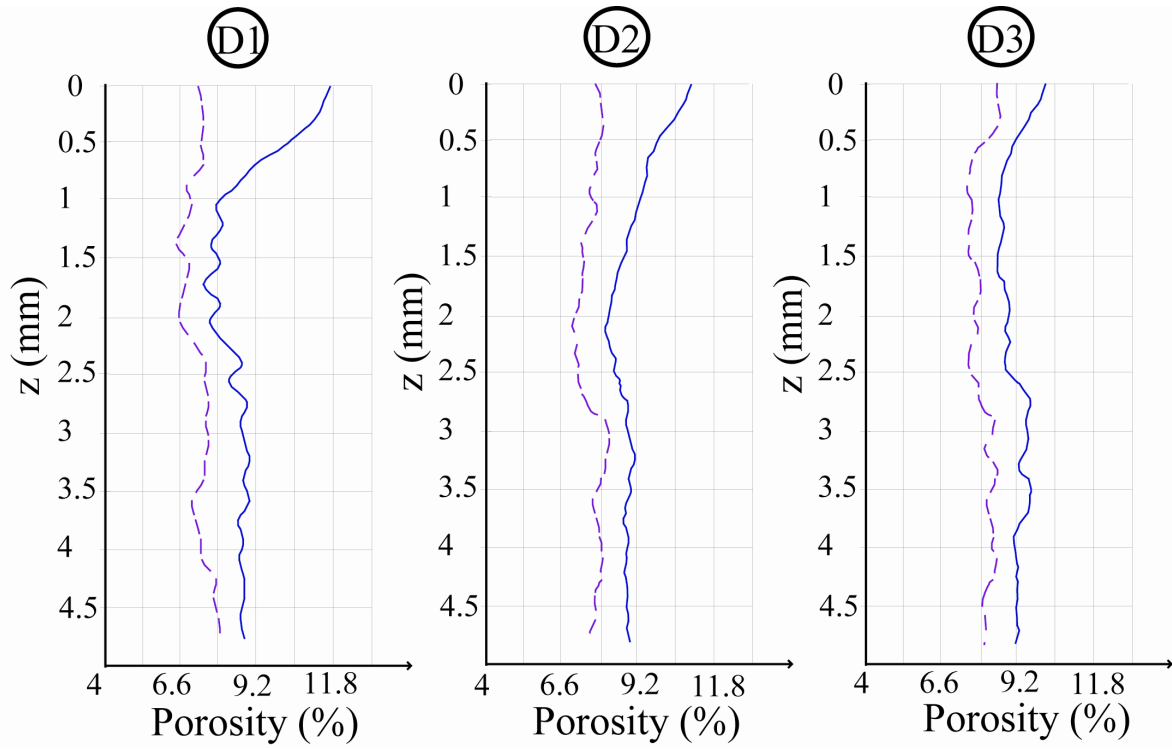
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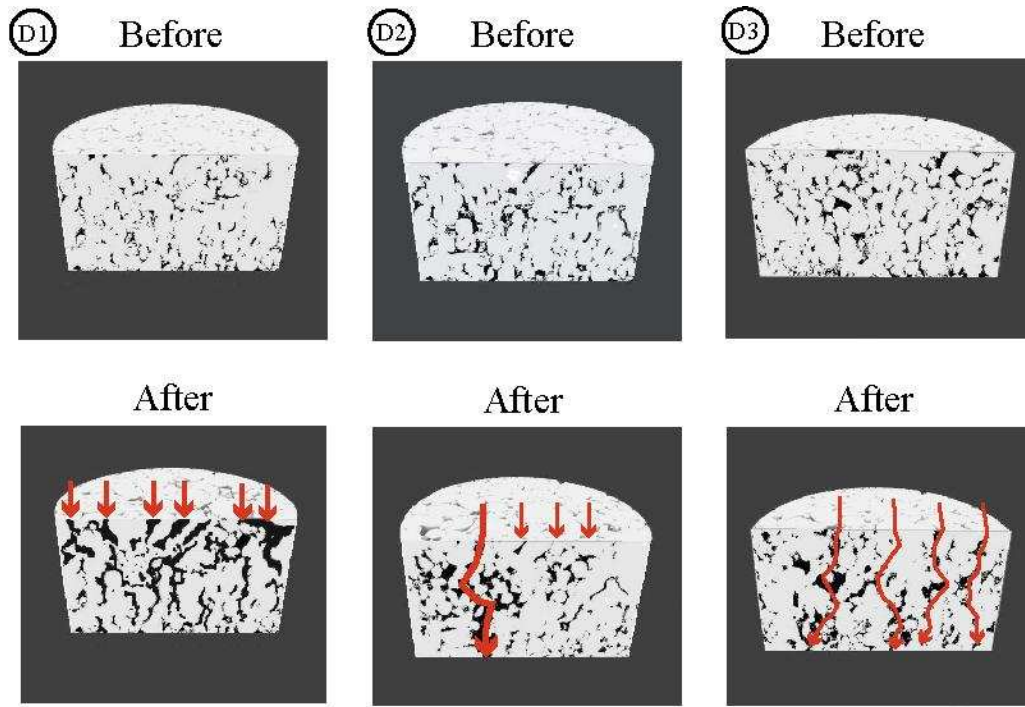
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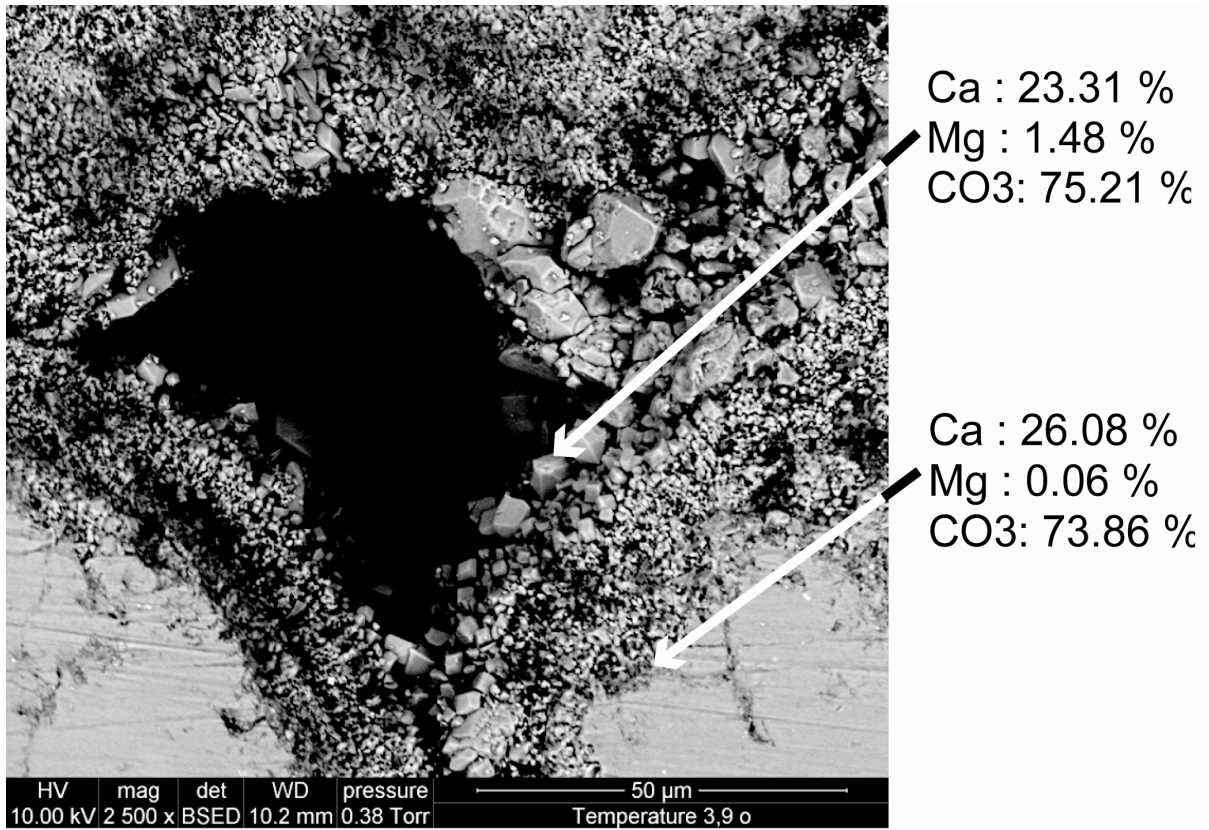
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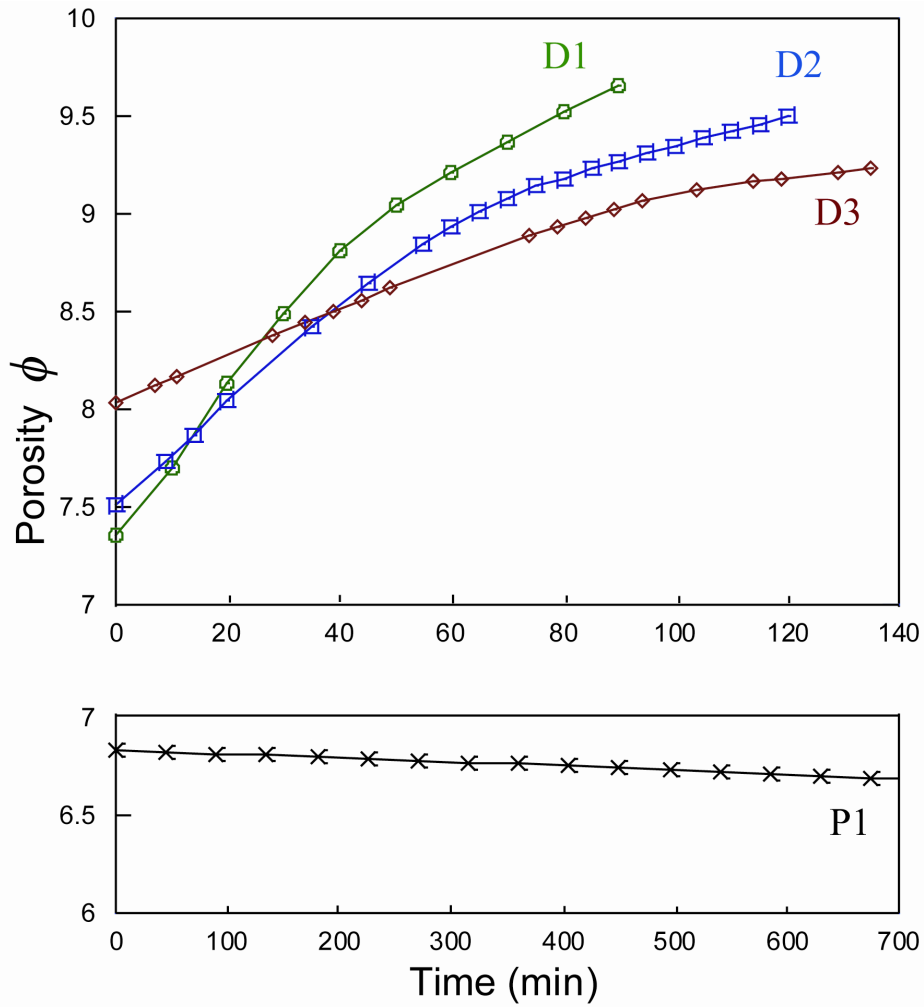


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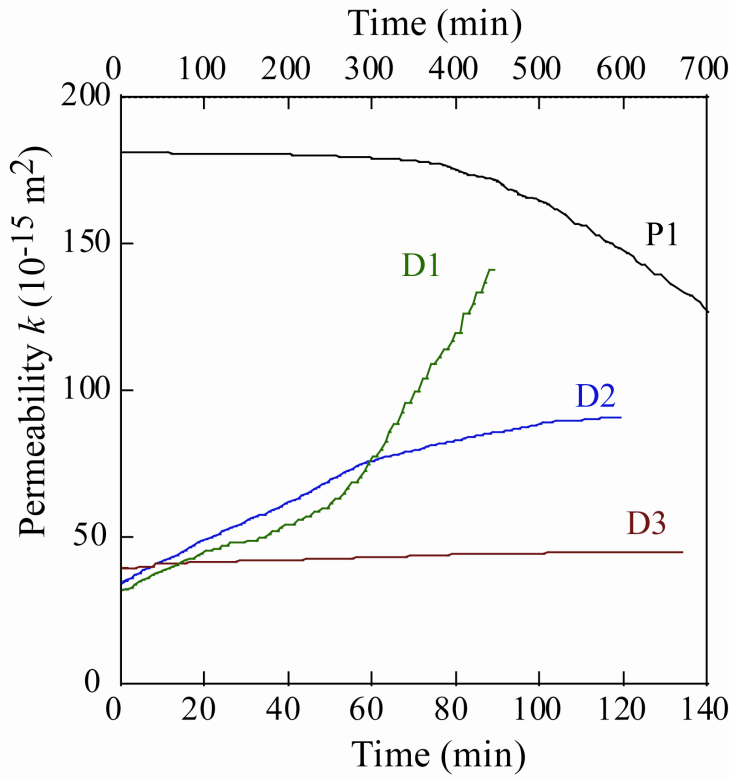
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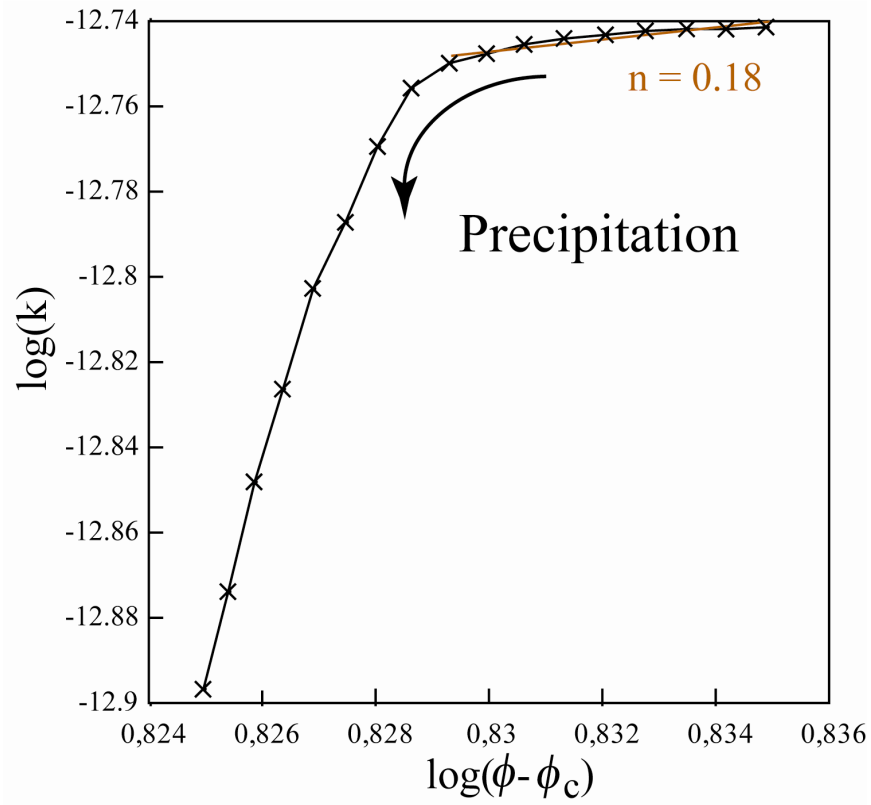
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**Fig. 11** : Variation of sample permeability with elapsed time for the dissolution experiments (D1 – D3) and the precipitation experiment P1.

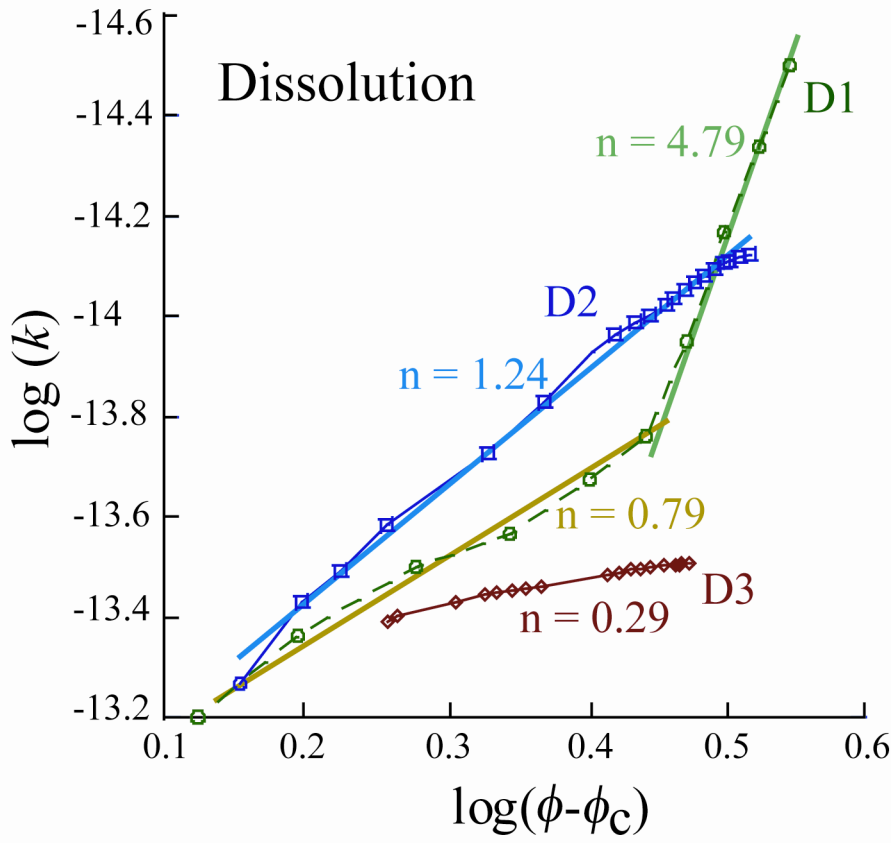


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**Fig. 12:** Log permeability versus log porosity for the precipitation experiments.



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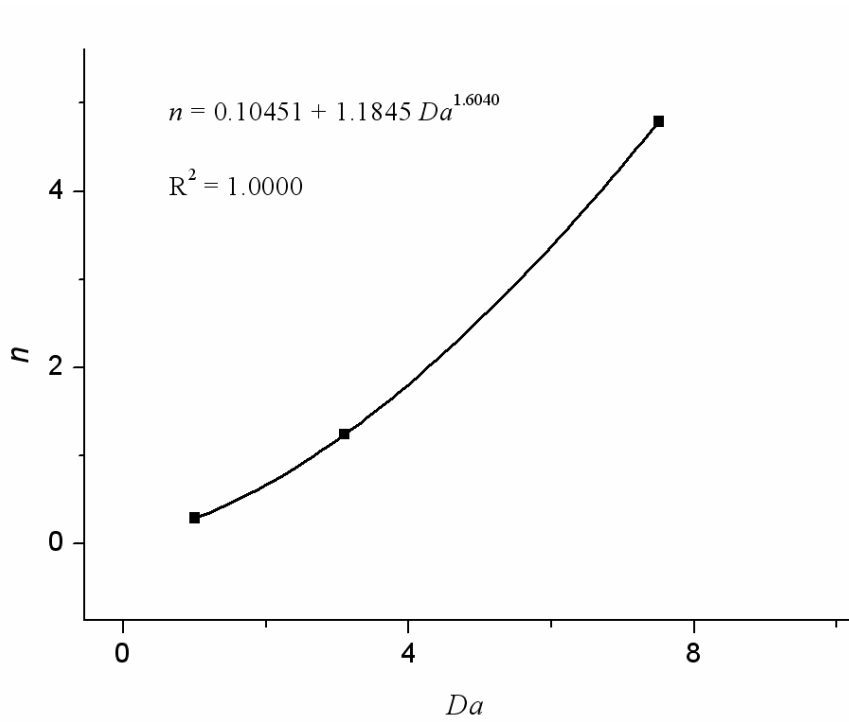


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