



It particularly results for the sample LNBV-1kt-2 (thin film without Zn):

$$(\Delta d/d)_{\perp} = 8.3 \cdot 10^{-4} \pm 2 \cdot 10^{-5}$$

$$a_{\perp \text{thin film}} = 0.51478 \text{ nm} \pm 2 \cdot 10^{-5} \text{ nm}$$

$$\text{with respect to } a_{\perp \text{substrate}} = 0.51522 \text{ nm} \pm 2 \cdot 10^{-5} \text{ nm}$$

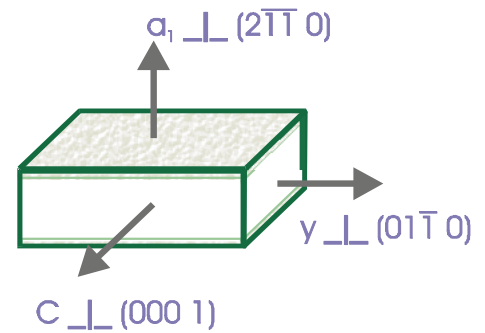
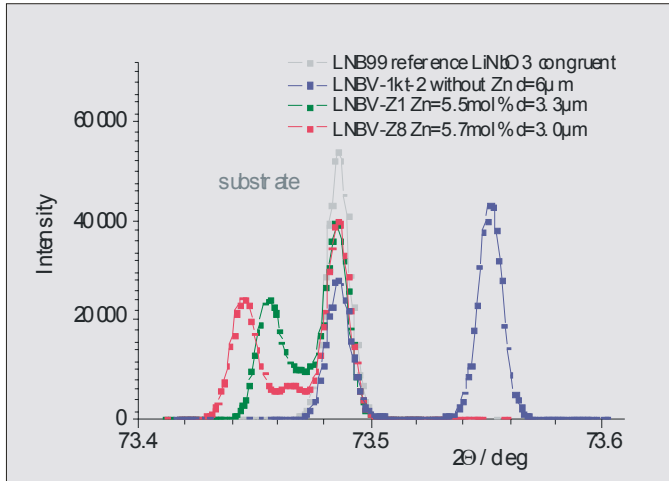


Fig. 1: $\Theta/2\Theta$ -scan taken up with the symmetric 4-2-2 0 - reflection of the LiNbO₃ thin film epitaxially grown on x-cut LiNbO₃ substrate

From two-dimensional 'reciprocal space maps' taken up by x-ray diffraction with asymmetric reflexes, data can be won both to the lateral and normal lattice parameters of the grown thin film in respect to the substrate, although with somewhat small precision ($\Delta d_{\parallel}/d_{\parallel} < 2 \cdot 10^{-4}$).



The rsm's (Fig. 2 and 3) reveals for the two different lateral directions $c_{\perp} (0001)$ and $y_{\perp} (01\bar{1}0)$ pseudomorphous growth of the thin film in respect to the substrate, despite the existing different crystallographic symmetry.

Using generalized Hooke' law in matrix way of writing, the relaxed lateral and normal lattice parameters as well as the deformation and tension components of the grown thin film can be computed.

$$\sigma_m = C_{mn} \epsilon_n \quad m, n = 1, \dots, 6$$

with $\sigma_2 \neq 0; \sigma_3 \neq 0; \sigma_1 = \sigma_4 = \sigma_5 = \sigma_6 = 0;$
 and $\epsilon_1 \neq 0; \epsilon_2 \neq 0; \epsilon_3 \neq 0; \epsilon_4 = \epsilon_5 = \epsilon_6 = 0;$

σ_m - tension components
 ϵ_n - deformation components
 C_{mn} - elastic stiffnesses / 10^9 Pa

$$\begin{aligned} \sigma_1 &= C_{11}\epsilon_1 + C_{12}\epsilon_2 + C_{13}\epsilon_3 \\ \sigma_2 &= C_{12}\epsilon_1 + C_{11}\epsilon_2 + C_{13}\epsilon_3 \\ \sigma_3 &= C_{13}\epsilon_1 + C_{13}\epsilon_2 + C_{13}\epsilon_3 \end{aligned}$$

and assuming that $\varepsilon_2 = \varepsilon_3$

$$\varepsilon_1 = - (C_{12} + C_{13}) / C_{13} \varepsilon_2$$

$$\varepsilon_1 = -0.64 \varepsilon_2 \quad (\leftarrow \text{transversal contraction})$$

C_{11} [10 ⁹ Pa]	C_{12} [10 ⁹ Pa]	C_{13} [10 ⁹ Pa]	C_{14} [10 ⁹ Pa]	C_{33} [10 ⁹ Pa]	C_{44} [10 ⁹ Pa]
203	55	75	8.8	244	60

Table 1: Elastic stiffness modulus [6] of LiNbO₃

From this follows the numerical calculation of the **relaxed lattice parameters** a_{relax} **und** c_{relax} for the stoichiometric LiNbO₃ thin film coherently grown on congruent LiNbO₃ substrates

with the measured values
especially for the sample LNBV-1kt-2 (thin film without Zn):

$$a_{\parallel} = 0.51522 \text{ nm}$$

$$a_{\perp} = 0.51478 \text{ nm}$$

$$c_{\parallel} = 1.3867 \text{ nm}$$

and with

$$(a_{\parallel} - a_{\text{relax}}) / a_{\text{relax}} = \varepsilon_{\parallel} = \varepsilon_2$$

$$(a_{\perp} - a_{\text{relax}}) / a_{\text{relax}} = \varepsilon_{\perp} = \varepsilon_1$$

$$\varepsilon_1 = -0.64 \varepsilon_2$$

$$a_{\text{relax}} = (a_{\parallel} - \varepsilon_2 / \varepsilon_1 \cdot a_{\perp}) / (1 - \varepsilon_2 / \varepsilon_1) = 0.5149 \text{ nm} \pm 0.0005 \text{ nm}$$

$$\varepsilon_1 = -3.49(1) \cdot 10^{-4}$$

$$\varepsilon_2 = 5.45(1) \cdot 10^{-4}$$

and with $(c_{\parallel} - c_{\text{relax}}) / c_{\text{relax}} = \varepsilon_{\parallel} = \varepsilon_3 (= \varepsilon_2)$

$$c_{\text{relax}} = 1 / (1 + \varepsilon_3) \cdot c_{\parallel} = 1.386 \text{ nm} \pm 0.002 \text{ nm}$$

$$\varepsilon_3 = 5.45(1) \cdot 10^{-4}$$

As final result arises now the 'in-plane' tension components of the grown thin film, in direction of the lateral crystallographic axes y and c, respectively

$$\sigma_2 = 1.32(1) \cdot 10^8 \text{ N/m}^2$$

$$\sigma_3 = 1.48(1) \cdot 10^8 \text{ N/m}^2$$

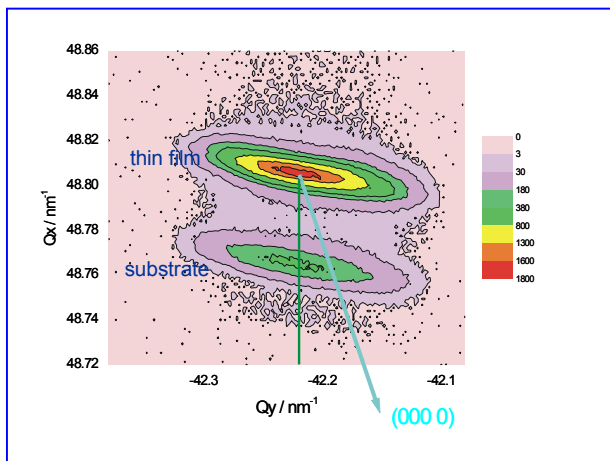


Fig 2: **rsm**: asymmetric 4-51 0-reflection

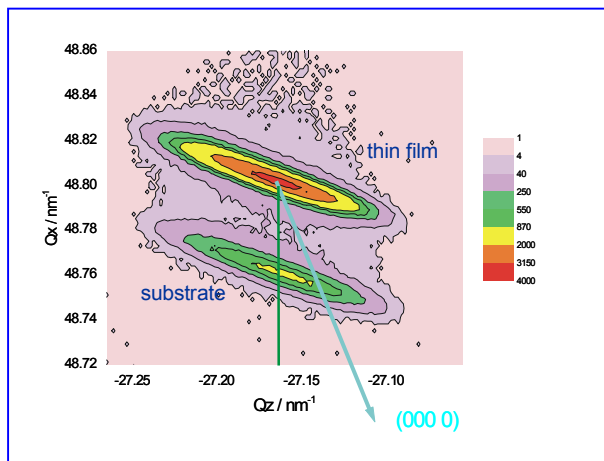


Fig 3: **rsm**: asymmetric 4-2-2 6-reflection

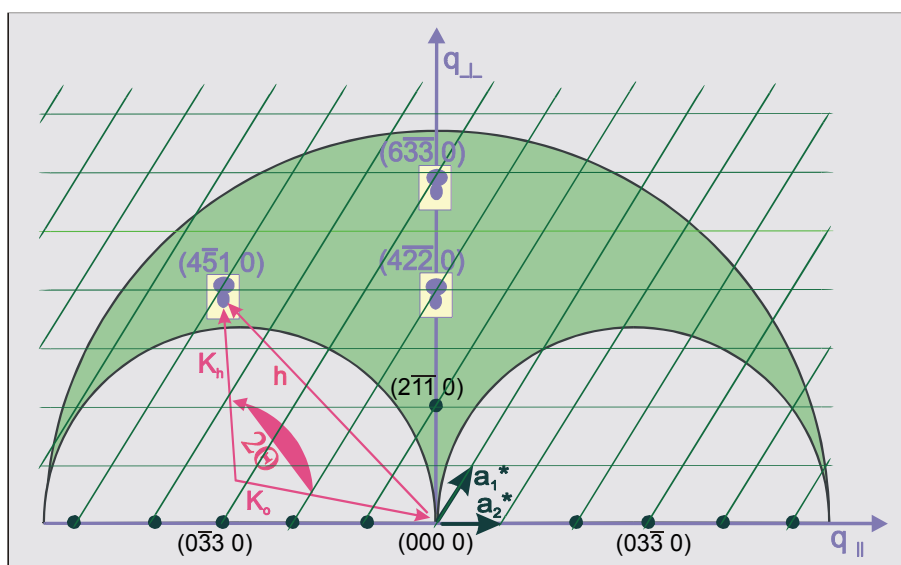


Fig. 4: Reciprocal lattice of LiNbO₃ in (000 1) cross-section projection for the two-dimensional taking up 'Reciprocal Space Maps' with asymmetric reflections to determine the lateral thin film lattice parameters in relation to the substrate.

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References

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