## XOP tutorial at ESRF - Session 1 Introduction to XOP

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## emission characteristics of synchrotron radiations sources

## 1. Bending Magnets

You will learn:

- to calculate bending magnet spectra using BM
- the basic use of Xplot

Simulate bending magnet spectra for different sources. Calculate numerical values, and fill them in the table below.
i) Maximum flux in number of photons (considering 1 mrad of horizontal aperture)
ii) Total power emitted by the BM in the full energy range.

Try to remember and check (or guess from numerical values)
iii) How the total power scales with the electrons energy?
iv) What is the power in the energy range from zero to the $E_{c}$ ? and from $E_{c}$ to infinity?

| Faciliy | E [GeV] | I [mA] | B [T]/R[m] | $\mathrm{E}_{\mathrm{c}}[\mathrm{eV}]$ | i (Flux) | ii (Total Power [W]) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ESRF | 6.04 | 200 | 0.8/25.2 |  |  |  |
| Elettra | 2 | 300 | 1.2/ 5.56 |  |  |  |
| LNLS | 1.37 | 175 | 1.67/2.74 |  |  |  |
| SLS | 2.4 | 400 | $\begin{aligned} & 1.45 \& 5 / \\ & 5.52 \& 1.6 \end{aligned}$ |  |  |  |
| APS | 7 | 100 | 0.6/ 38.9 |  |  |  |
| NSLS | 2.58 | 500 | 0.77/ 11.2 |  |  |  |
| SSRL | 3 | 100 | 1.22/8.20 |  |  |  |

Information source:
ESRF: www.esrf.fr
Elettra: http://www.elettra.trieste.it/about/parameters.html
LNLS: ttp://www.lnls.br/info/info.htm
SLS: http://www1.psi.ch/www sls hn/sls accelerator.htmlx
Others: http://www-als.lbl.gov/als/intersrc/existing.html

## Hints:

Use $X O P \mid$ Bending Magnet $\mid B M$ to create the spectra. Numerical values can be obtained from the resulting $B M \mid$ Show $\mid$ View Results window and plots can be done using $B M \mid$ Show $\mid$ Plot Results, which creates a graphical window (Xplot). Power values can be calculated by integrating the power density spectra or read directly from the results window.
Integration of the power spectrum can be done with Xplot $\mid$ Calculations $\mid$ Width/Integral/MinMax menu. For integrating over a limited range of abscissas, just select the desired interval with Xplot $\mid$ Edit $\mid$ Limits $\mid$ Set... and the apply the Xplot $\mid$ Calculations $\mid$ Width/Integral/MinMax again.
The questions iii) and iv) can be answered without using the computer. Question iv) can be checked by calculating the normalized cdf(power spectrum) using first Xplot $\mid$ Calculations $\mid c d f$ to calculate $\operatorname{cdf}$ (power spectrum) and then normalizing the result with Xplot $\mid$ Calculations $\mid$ Operations with columns

## 2. Conventional wigglers

You will learn:

- to calculate standard wiggler spectra using Xwiggler and WS.
- understand the pros and cons of each program
- use applications input files

Simulate spectra for different ESRF conventinal wigglers. Calculate
i) Maximum flux (for $\mathrm{I}=200 \mathrm{~mA}$ )
ii) Critical Energy corresponding to maximum deflection (from Show parameters)
iii) Calculate the effective critical energy with Xplot
iv) Total emitted power (for I=200 mA)
$\left.\begin{array}{|l|l|l|l|l|l|l|}\hline & \boldsymbol{\lambda}_{\mathbf{u}}[\mathbf{m}] & \mathbf{K} & \mathbf{N} & \begin{array}{l}\text { Max Flux } \\ \text { ph/sec/0.1\%bw }\end{array} & \text { Ec }[\mathrm{eV}] & \begin{array}{ll}\text { Tot } & \text { Power } \\ \text { at } & \mathrm{I}=200 \\ \mathrm{~mA}\end{array} \\ {[\mathrm{~kW}]}\end{array}\right]$

Used symbols:
$\lambda_{u}$ : magnetic period of the insertion device
N : number of periods
K : deflection parameter
Information source: http://www.esrf.fr/machine/support/ids/Public/Ids/installed_IDs.html and beamline web pages

Hints: Use the Xop|Sources|wigglers|Xwiggler to create the spectra. Make calculations, for instance, from 100 to 100000 eV with 200 eV step. Save the flux spectrum of id9 in an ASCII file (for comparison with results of undulator model, to be done later).
Use the Xop|Sources|wigglers|Ws for calculating the spectrum of id11. Compare with previous results.
Use Xplot|Calculations|Width/Integral/MinMax to get maxima. The effective critical energy can be calculates using the normalized $\operatorname{cdf}(f l u x)$, as done before.

## 3. Asymmetric wiggler (id20)

You will learn:

- to calculate the flux of asymmetric wiggler spectra using Xwiggler
- Use magnetic field from $\mathrm{B}(\mathrm{y})$ map or from harmonic decomposition.

Calculate the emission spectrum of an asymmetric wiggler
i) Calculate the maximum flux and the total emitted power XWIGGLER
ii) Calculate B as a function of the harmonics (use Xop|Tools|Xop macro, load and run the file xwiggler_id20.mac)

|  | $\boldsymbol{\lambda}_{\mathbf{u}}[\mathbf{m}]$ | $\mathbf{K}$ | $\mathbf{N}$ | Max <br> ph/sec/0.1\%bw | Flux | Ec [eV] | Tot <br> Power $^{*}$ <br> $[\mathrm{~kW}]$ |
| :--- | :--- | :--- | :--- | :--- | :---: | :--- | :--- |
| Id20(asym) | $\mathbf{0 . 2 1 0}$ | $\mathbf{1 5}$ | $\mathbf{8}$ |  |  |  |  |

Hints: Use Xop|Xwiggler. The magnetic field data for Id20 is available in the files xwiggler_h.dat or xwiggler_b.dat (harmonics and magnetic field, respectively).

## 4. Undulator sources (angular distribution)

## You will learn:

- to calculate the angular distribution of the undulator emission using Xurgent and Xus
- to calculate and visualize the effect of electron beam emittances.
a) Calculate the distribution of flux (at an energy corresponding to the first harmonic, $\mathrm{E}=166.8 \mathrm{eV}$ ) versus emission angle for the yellow book example (no emittance, $\mathrm{N}=14, E_{e}=1.3 \mathrm{GeV}, \lambda_{u}=3.5 \mathrm{~cm}, \mathrm{~K}=1.87$ ). Use Xurgent and Xus
ii) Calculate the distribution of flux (at an energy corresponding to the first harmonic) versus emission angle for ESRF U46 ( $E_{e}=6.04 \mathrm{GeV}, \mathrm{N}=35, \lambda_{u}=46 \mathrm{~mm}, \mathrm{~K}=2.76$ ) in three cases: i) no emittance, ii) undulator placed in an ESRF high beta section, and iii) low beta. Use Xus (and Xurgent)

|  | High Beta | Low beta | BM |
| :--- | :--- | :--- | :--- |
| $\sigma_{x}[\mu \mathrm{~m}]$ | 395 | 57 | 126 |
| $\sigma_{z}[\mu \mathrm{~m}]$ | 9.9 | 10.3 | 36.9 |
| $\sigma_{x}[\mu \mathrm{rad}]$ | 10.5 | 88.3 | 108 |
| $\sigma_{z}[\mu \mathrm{rad}]$ | 3.9 | 3.8 | 1.1 |

Information source: http://www.esrf.fr/machine/support/ids/Public/Sizes/sizes.html

## 5. Undulator sources (flux and spectral density)

You will learn:

- to calculate the photon flux, spectral density and total power emission of undulators
i) Calculate the flux and spectral power spectra for the three insertion devices of id9 (low beta). Use a $3 \times 3 \mathrm{~mm}^{2}$ slit placed at 27 m from the source. Give the maximum flux and total power.
ii) Compare the W70 flux with the result obtained with the wiggler model.

|  | N | K | $[\mathrm{mm}]$ | Power [W] | Flux |
| :--- | :--- | :--- | :--- | :--- | :--- |
| U20 | 81 | 0.27 | 20 | 45.5 | 6.38 e 13 |
| U46 | 36 | 2.76 | 46 | 571.8 | 1.88 e 14 |
| W70 | 22 | 5.43 | 70 | 472.0 | 9.45 e 13 |

Hints: Use Xop|Sources|Undulator|Xurgent and/or Xop|Sources|Undulator|Xus. Compare results. Check power results with web data at: http://www.esrf.fr/exp facilities/ID9/id9.html

## 6. Filters and mirrors: effect on source

You will learn:

- to save an Xop source to files to be used with Xpower
- to calculate filter transmission and mirror reflectivity and to see their effects on the source spectrum.
- evaluate absorbed and transmitted power

Calculate how a $500 \mu \mathrm{~m}$ Be window plus a Rh mirror (set at 3 mrad of grazing angle) modify the BM flux calculated in the previous exercise 1. Calculate the absorbed power by these elements. Add other filters (e.g., Al, Mo, etc).

Hints: From the $X o p \mid B M$ window used previously, create the files with the source spectra by using BM|File|Write files for xop/Optics. Open the Xop $\mid$ Optics $\mid$ Mirrors\&Filteres $\mid X P O W E R$ application. From the main parameter window, select the source to either xop/source Flux or xop|source Power. Fill-in the
 results. Use Show|Cumulative transmission to see the sequential effect of the optical elements on the source. Use the Xplot $\mid$ Save button to overplot the spectra after the different elements.

## 7. Crystal monochromators

You will learn:

- calculate diffraction profiles of perfect crystals
- calculate the response of two crystals (+,-) (curve multiplication)
- calculate rocking curves (convolution)
- calculate harmonic suppression
i) Calculate the diffraction profiles, Bragg angle, width, peak and integrated reflectivity of Si 111 at the energies $5 \mathrm{keV}, 8 \mathrm{keV}, 12 \mathrm{keV}, 50 \mathrm{keV}, 80 \mathrm{keV}$ and 120 keV .
ii) For the 8 keV case, calculate the diffracted profile of a double Si111 reflection in $(+,-)$ configuration. Calculate the rocking curve resulting of the rotation of the second crystal respect to the first one.
iii) For a Si111 double crystal monochromator at 8 keV , calculate the angular tilt of the second crystal needed to suppress the third harmonic reflection.

Hints: Use the $X o p \mid$ Optics $\mid$ Crystals $\mid$ XCrystal application to create the profiles. The peak, width and integrated reflectivity values can be obtained using Xplot $\mid$ Calculations $\mid$ Width/Integral/MinMax on each profile. For the double reflection $(+,-)$ one should multiply a given diffraction profile by itself using the Xplot $\mid$ Calculations $\mid$ Operations with columns item. Use Xplot $\mid$ Save Plot button to overplot the new curve on the original one. The rocking curve is calculated by convoluting the diffraction profile with itself. For doing that, use the Xplot $\mid$ Calculations $\mid$ Convolution and Correlation entry, and make autoconvolution normalized to the second set.
For the harmonic supression one should calculate the main Sil11 reflection at 8 keV and the third harmonic (Si333 at 24 keV ). Check that both cases give the same Bragg angle. Keep two Xplot windows, one for each profile. Estimate the misalignments one must introduce to supress the Si333 reflection (should be larger than the diffraction profile width). Create a new set of data for the shifted Si333 reflection by changing the angular (abscissas value with Xplot $\mid$ Calculations $\mid$ Operations with sets. Save the result to a file. Multiply the original Si333 reflection by the shifted one using the Xplot $\mid$ Calculations $\mid$ Operations with sets of the Xplot window of the original Si333 Xplot window. Repeat the process of shifting with the main reflection Sil11 using the same value of angular misalignment. Calculate the new peak, width and integrated reflectivity, and compare with the double non-misaligned reflection $(+,-)$.

## 8. Bent crystals

You will learn:

- to calculate diffractions profiles of bent crystals
- understand the limitations of the available models
- to see the transition from dynamical to kinematical theory
i) Calculate the deformation of Si111 symmetric Bragg diffraction profile at 12 keV for different values of the bending radius (from 100 m to 5 cm ). For each curve calculate the integrated reflectivity and see the transition from the Dynamic theory value ( $\mathrm{R} \gg$ ) to the Kinematical theory value ( $\mathrm{R} \ll$ ).
ii) Calculate the diffraction profile in Laue for Si111 at 33 keV and asymmetry angle $a=63.78 \mathrm{deg}$, and curvature radius 13 m .

Hints: Use Xop $\mid$ Crystals $\mid$ Crystal_bent application. Use the "multilamellar" theory for the Bragg reflection and the "Penning\&Polder" theory for the Laue system.

## 9. Reflectivity curves of multilayers.

You will learn to:

- use Mlayer to calculate reflectivity from simple multilayers
- understand the limitations of Mlayer
- start and use IMD as Xop extension
- understand the basic features of multilayer reflectivity spectra
i) Using MLAYER calculate the reflectivity as a function of grazing angle, from zero to 6 deg , of $[\mathrm{W}(25 \AA) / \mathrm{Si}(25 \AA)] \times 50$ on Si at an energy of 8050 eV
ii) Using IMD, using no slope errors (if not specified), calculate the following reflectivity spectra at $\mathrm{E}=8050 \mathrm{eV}$ :

1. $[\mathrm{W}(25 \AA) / \mathrm{Si}(25 \AA)] \times 50$ on Si
2. $[\mathrm{W}(10 \AA) / \mathrm{Si}(40 \AA)] \times 50$ on Si
3. $[\mathrm{W}(5 \AA) / \mathrm{Si}(45 \AA)] \times 50$ on Si
4. $[\mathrm{W}(25 \AA) / \mathrm{Si}(25 \AA)] \times 10$ on Si
5. $[\mathrm{W}(25 \AA) / \mathrm{Si}(25 \AA)] \times 50$ on Si , roughness $\sigma=5 \AA$
6. $\mathrm{SiO}(90 \AA)[\mathrm{W}(5 \AA) / \mathrm{Si}(45 \AA)] \times 50$ on Si

Comment the results.

## 10. Quick tour to other applications

Open and run the following applications:

- DABAX main interface and applications
- XXCOM
- MAMON
- CRL


## Appendix - Useful formulas

## Bending Magnet:

$$
\begin{gather*}
E[e V]=\frac{12398.52}{\lambda[\AA]}  \tag{1.1}\\
\gamma=\frac{E_{e}}{m_{e} c^{2}}=\frac{E_{e}[\mathrm{GeV}]}{511.0034 \cdot 10^{-6} \mathrm{GeV}}=1956.93 E_{e}[\mathrm{GeV}]  \tag{1.2}\\
B[T]=\frac{3.334728 E_{e}[\mathrm{GeV}]}{R[\mathrm{~m}]} \tag{1.3}
\end{gather*}
$$

Critical energy and wavelength

$$
\begin{equation*}
\lambda_{c}=\frac{4 \pi}{3} \frac{R}{\gamma^{3}} ; \quad E_{c}[\mathrm{keV}]=0.665 E_{e}^{2}[\mathrm{GeV}] B[T] \tag{1.4}
\end{equation*}
$$

Power emitted

$$
\begin{equation*}
P[\mathrm{~W} / \mathrm{mrad}]=\frac{88.46278 E_{e}^{4}[\mathrm{GeV}] I[\mathrm{~A}]}{2 \pi R[\mathrm{~m}]} \tag{1.5}
\end{equation*}
$$

## Wiggler and Undulators:

$$
\begin{equation*}
K=0.934 \lambda_{u}[\mathrm{~cm}] B[T] \tag{1.6}
\end{equation*}
$$

First harmonic energy:

$$
\begin{equation*}
\varepsilon_{1}[\mathrm{keV}]=0.950 \frac{E^{2}[\mathrm{GeV}]}{\left(1+\frac{K^{2}}{2}\right) \lambda_{u}[\mathrm{~cm}]} \tag{1.7}
\end{equation*}
$$

Central cone width of the $n$-th harmonic:

$$
\begin{equation*}
\sigma_{r^{\prime}}=\frac{1}{\gamma} \sqrt{\frac{1+\frac{K^{2}}{2}}{2 N n}}=\sqrt{\frac{\lambda / n}{L}} \tag{1.8}
\end{equation*}
$$

Position of the $l$-th ring:

$$
\begin{equation*}
\theta_{n, l}=\frac{1}{\gamma} \sqrt{\frac{l}{n}\left(1+\frac{K^{2}}{2}\right)} \tag{1.9}
\end{equation*}
$$

Total radiated power

$$
\begin{equation*}
P[k W]=0.633 E^{2}[\mathrm{GeV}] B_{0}^{2}[T] L[m] I[A] \tag{1.10}
\end{equation*}
$$

## Answers

## 1 - Bending magnets

Use the XOP input files bm_* . xop

| Faciliy | $\mathbf{E}[\mathbf{G e V}]$ | $\mathbf{I}[\mathbf{m A}]$ | $\mathbf{B}[\mathbf{T}] / \mathbf{R}[\mathbf{m}]$ | $\mathrm{E}_{\mathrm{c}}[\mathrm{eV}]$ | $\mathrm{i}($ Flux $)$ | ii (Total Power [W]) |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| ESRF | $\mathbf{6 . 0 4}$ | $\mathbf{2 0 0}$ | $\mathbf{0 . 8 / \mathbf { 2 5 . 2 }}$ | 19414 | 2.72 e 13 | 149.9 |
| Elettra | $\mathbf{2}$ | $\mathbf{3 0 0}$ | $\mathbf{1 . 2 / \mathbf { 5 . 5 6 }}$ | 3193 | 1.34 e 13 | 12.16 |
| LNLS | $\mathbf{1 . 3 7}$ | $\mathbf{1 7 5}$ | $\mathbf{1 . 6 7 / \mathbf { 2 . 7 4 }}$ | 2085 | 5.41 e 12 | 3.17 |
| SLS | $\mathbf{2 . 4}$ | $\mathbf{4 0 0}$ | $\mathbf{1 . 4 5 \mathbf { 8 } \mathbf { 5 } /}$ | $5555.7 \&$ | $5.41 \mathrm{e} 12 \&$ | $33.87 \&$ |
|  |  |  | $\mathbf{5 . 5 2} \mathbf{\& 1 . 6}$ | 19158 | 2.16 e 13 | 116.8 |
| APS | $\mathbf{7}$ | $\mathbf{1 0 0}$ | $\mathbf{0 . 6 / \mathbf { 3 8 . 9 }}$ | 19557 | 1.58 e 13 | 86.9 |
| NSLS | $\mathbf{2 . 5 8}$ | $\mathbf{5 0 0}$ | $\mathbf{0 . 7 7 / \mathbf { 1 1 . 2 }}$ | 3409.4 | 2.90 e 13 | 27.9 |
| SSRL | $\mathbf{3}$ | $\mathbf{1 0 0}$ | $\mathbf{1 . 2 2 / 8 . 2 0}$ | 7303.8 | 6.77 e 12 | 13.91 |

iii) How the total power scales with the electrons energy?

Proportional to $\mathrm{E}^{4}$ when keeping constant the bending radius R
iv) What is the power in the energy range from zero to the Ec? and from Ec to infinity? $\mathrm{P}\left[0, \mathrm{E}_{\mathrm{c}}\right]=\mathrm{P}\left[\mathrm{E}_{\mathrm{c}}, \infty\right]=0.5$ Total Power

## $\underline{2}$ - Conventional wigglers

use the XOP input files:

```
xwiggler_id9.xop
xwiggler_id11.xop and ws_id11.xop
xwiggler_id17.xop
```

|  | $\boldsymbol{\lambda}_{\mathbf{u}}[\mathbf{m}]$ | $\mathbf{K}$ | $\mathbf{N}$ | Bmax <br> $[\mathbf{T}]$ | Max Flux <br> ph/sec/0.1\%bw | Ec [eV] | Tot Power <br> at I=200 <br> mA $[\mathrm{kW}]$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Id9 | $\mathbf{0 . 0 7 0}$ | $\mathbf{5 . 4 3}$ | $\mathbf{2 2}$ | $\mathbf{0 . 8 3}$ | 1.06 e 15 | 20204 <br> web:2000 | 4.86 <br> web 4.74 |
| Id11 | $\mathbf{0 . 1 2 5}$ | $\mathbf{1 4 . 7}$ | $\mathbf{1 2}$ | $\mathbf{1 . 2 4}$ | 1.58e15 at 5.1keV <br> (web 1.4e17??) | 30631 <br> (web 29000) | 10.415 <br> (web:20) |
| Id17 | $\mathbf{0 . 1 5 0}$ | $\mathbf{1 9 . 6}$ | $\mathbf{1 1}$ | $\mathbf{1 . 5 - 1 . 4}$ | 2.11e15 | 34034 <br> (web:33500) | 13.9 <br> (web:14.3) |

## 3 - Asymmetric wiggler (id20)

Use the XOP input files:

```
xwiggler_id20_b.xop
xwiggler_id20_h.xop
```

$\left.\begin{array}{|l|l|l|l|l|l|l|l|}\hline & \boldsymbol{\lambda}_{\mathbf{u}}[\mathbf{m}] & \mathbf{K} & \mathbf{N} & \text { Bmax[T] } & \begin{array}{l}\text { Max } \\ \text { ph/sec/0.1\%bw }\end{array} & \text { Flux } & \text { Ec [eV] }\end{array} \begin{array}{l}\text { Tot } \\ \text { Power } \\ {[\mathrm{kW}]}\end{array}\right]$.

## 4 - Undulator sources (angular distribution)

Use the XOP input files:

```
xurgent_yellowbook.xop and xus_yellowbook.xop
xurgent_hb_u46.xop and xus_hb_u46.xop
xurgent_lb_u46.xop and xus_lb_u46.xop
```

In Xus the results are under Xus|Show|Plot 3D surface|Total intensity

## 5 - Undulator sources (flux and spectral density)

i) Use the files:

```
xurgent_id9_u20.
xurgent_id9_u46.xop
xurgent_id9_w70.xop
```

ii) For comparison, integrate over $1 \times 0.5 \mathrm{mrad}^{2}$ :

URGENT2.0, File: urgent.out, $\mathrm{Ky}=5.43000$, ALL HARMONICS


## 6 - Filters and mirrors: effect on source

use the XOP input file xpower. xop

## 7 - Crystal monochromators

i)

| Crystal | $\begin{aligned} & \mathrm{E} \\ & {[\mathrm{keV}]} \end{aligned}$ | $\begin{aligned} & \hline \theta_{\mathrm{B}} \\ & {[\mathrm{deg}]} \\ & \hline \end{aligned}$ | W[ $\mu \mathrm{rad}$ ] | Peak | $\begin{aligned} & \text { Integ } \\ & \text { Int } \\ & \hline \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Sil11 | 5 | 23.3 | 61.3 | 0.86, | 60 |
| Si111 | 8 | 14.3 | 36.5 | 0.94, | 40 |
| Si111 | 12 | 9.5 | 23.8 | 0.97, | 28 |
| Sil11 | 50 | 2.27 | 5.55 | 1.00, | 6.7 |
| Sil11 | 80 | 1.42 | 3.48 | 1.00, | 4.2 |
| Sil11 | 120 | 0.94 | 2.31 | 1.00, | 2.9 |

ii) Continuous line: convolution (rocking curve). Dashed line: single reflection. Dotted line: double reflection

iii)

Si333 single reflection: $\mathrm{W}=3.1, \mathrm{P}=0.99$, $\mathrm{I}=3.45 \Rightarrow$ Shifting $3.5 \mu \mathrm{rad}$
Si333.Si333(shifted): $\mathrm{W}=3.1, \mathrm{P}=0.07, \mathrm{I}=0.24$
Si111.Si111: W=33.8, $\mathrm{P}=0.88, \mathrm{I}=29.2$
Si111.Si111(shifted): $\mathrm{W}=32.3, \mathrm{P}=0.88, \mathrm{I}=28.4$

## 8 - Bent crystals

i)

| R[cm] | FWHM[mrad] | Integrated <br> reflectivity |
| :--- | :--- | :--- |
| 5 (dashed) | 92 | 0.395 |
| 25 | 0.39 | 0.300 |
| 50 (dotted) | 0.19 | 0.22 |
| 100 | 0.11 | 0.136 |
| 2000 (cont) | 0.03 | 0.97 |


ii)


## 9 - Reflectivity curves of multilayers

i) Use the file mlayer.xop
ii) Start with the file imdWSi.dat.






*)
*)

The following features can be observed:

1) A plateau corresponding to the total reflection zone.
2) Outside the plateau, the background decreases with $q^{-4}$. Changes in this background are due to the roughness in the interfaces and experimental background.
3) Satellite maxima. The angular spacing depends on the bilayer periodicity d. Their angular separation is determined by the Bragg law. If the spectrum extends over many peaks, it is possible to observe absences of some peaks, which are related to $\Gamma$. Peaks at $\Gamma^{-1}$ are absent.
4) Kiessig fringes, which period depends on the total multilayer thickness (i.e., number of bilayers).
5) If a top or capping layer exists (usually an oxide layer) it creates side maxima close
to the satellites.
6) The satellite width is proportional to $1 / \mathrm{N}, \mathrm{N}$ being limited by the absorption of the stack. Although the theoretical width is the same for all satellites, in experimental measurements one usually sees an increase of the satellite width as the satellite order increases.
7) The effect of increasing $N$ is also to increase peak intensity in satellites. This is limited by the roughness and stack absorption.
